

Dark Matter in the Milky Way’s Dwarf Spheroidal Satellites

Matthew G. Walker^{1,2}

ABSTRACT

The Milky Way’s dwarf spheroidal satellites include the nearest, smallest and least luminous galaxies known. They also exhibit the largest discrepancies between dynamical and luminous masses. This article reviews the development of empirical constraints on the structure and kinematics of dSph stellar populations and discusses how this phenomenology translates into constraints on the amount and distribution of dark matter within dSphs. Some implications for cosmology and the particle nature of dark matter are discussed, and some topics/questions for future study are identified.

1. Introduction

Physics assigns to gravity the responsibility of forming structure on scales ranging from terrestrial to cosmological. An apparent threshold arises somewhere between scales characteristic of star clusters and those characteristic of galaxies. The internal dynamics of gravitationally bound structures smaller than a few parsecs, of which globular clusters are the largest examples, are reasonably well described in terms of standard gravity (i.e., Einstein’s general theory and/or its Newtonian approximation) sourced by known substances. The internal dynamics of gravitationally bound structures larger than a few tens of parsecs, of which dwarf spheroidal (dSph) galaxies are the smallest examples, are not.

The ubiquity of dark matter on galactic and larger scales signifies new physics. Either there exists an otherwise unknown substance that contributes to dynamical mass but not to baryonic mass, or the standard dynamical framework requires modification (or both). The ‘substance’ hypothesis is not falsifiable, but in principle it can be confirmed with the detection of non-gravitational interactions involving dark matter particles. In any case, dSphs provide the most extreme examples of dark matter phenomenology, with dynamical mass-to-light ratios $M/L_V \gtrsim 10 [M/L_V]_\odot$ even at their centers. This fact has made dSphs the focus of intense scrutiny in the effort to understand the nature of dark matter.

This article reviews the development of empirical constraints on the amount and distribution of dark matter within the Milky Way’s dSph satellites. These results follow from the application of

¹Harvard-Smithsonian Center for Astrophysics, 60 Garden St., Cambridge, MA 02138

²Hubble Fellow

a rich variety of analyses applied to observations conducted by many individuals and groups. All analyses described here are formulated within the Newtonian dynamical framework. The reader is welcome to interpret ‘dark matter’ in terms of the substance hypothesis or more generally as a quantification of the discrepancy between dynamical and baryonic mass. The focus here is on the relationship between data and constraint, and one hopes that this information translates meaningfully into alternative dynamical frameworks (as formulated, e.g. by Bergmann 1968; Milgrom 1983; Bekenstein 2004; Moffat 2006).

2. Observations

Bright red giant stars are detectable as point sources with $m_V \lesssim 21$ mag out to distances of ~ 0.5 Mpc. Within this range, the Milky Way’s dSph galactic satellites appear as localised over-densities of individually resolved stars. Empirical information about the number, stellar structure and internal kinematics of these systems has steadily accumulated for the past eight decades.

2.1. Census

Shapley (1938a) discovered the Sculptor dSph upon visual examination of a photographic plate exposed for three hours with the 24-inch Bruce telescope at (what was then) Harvard’s Boyden observatory in South Africa. In this original dSph discovery paper, Shapley notes that Sculptor is visible—in hindsight—as a faint patch of light on a plate taken for the purpose of site testing, in 1908, during a series of five exposures totalling nearly 24 hours with a 1-inch refracting telescope.

Reporting shortly thereafter the similar discovery of Fornax, Shapley (1938b) notes that the new type of ‘Sculptor-Fornax’ cluster shares properties with both globular clusters and elliptical galaxies, then speculates that ‘At the distance of the Andromeda system these objects would, in fact, have long escaped discovery. There may be several others in the Local Group of galaxies; such objects may be of frequent occurrence in intergalactic space and of much significance both in the census and the genealogy of sidereal systems.’

Figure 1 demonstrates Shapley’s prescience, plotting the cumulative number and luminosities of the Milky Way’s known dSph satellites against date of discovery publication. Harrington & Wilson (1950) and Wilson (1955) found the next four ‘Sculptor-type’ (as they were then called) systems—Leo I, Leo II, Draco and Ursa Minor—on photographic plates taken for the Palomar Observatory Sky Survey with the 48-inch Schmidt telescope. Cannon et al. (1977) spotted Carina by eye on a plate taken with the 1.2-meter UK-Schmidt Telescope. Irwin et al. (1990) used the Automated Photographic Measuring (APM) facility at the University of Cambridge to detect Sextans, again on a UK-Schmidt plate, thereby completing the census of the Milky Way’s eight so-called ‘classical’ dSphs.

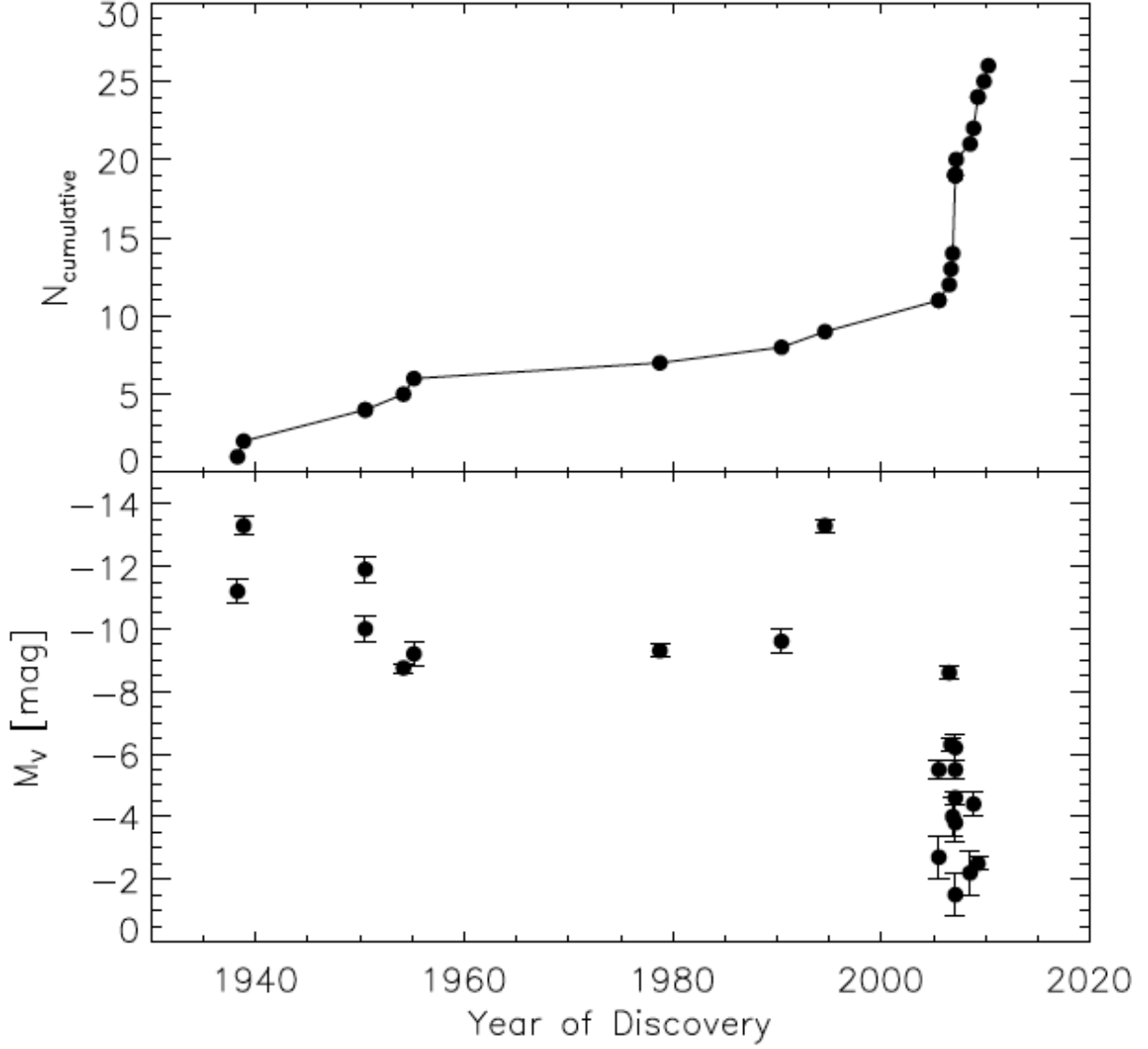


Fig. 1.— Cumulative number (top) and luminosity (bottom) of known dwarf spheroidal satellites of the Milky Way, versus year of publication of discovery paper (Shapley 1938a,b; Harrington & Wilson 1950; Wilson 1955; Cannon et al. 1977; Irwin et al. 1990; Ibata et al. 1994; Willman et al. 2005b,a; Belokurov et al. 2006; Zucker et al. 2006b,a; Belokurov et al. 2007; Irwin et al. 2007; Walsh et al. 2007; Belokurov et al. 2008; Belokurov et al. 2009; Grillmair 2009; Watkins et al. 2009; Belokurov et al. 2010).

The next discovery was unique in that it came via spectroscopy rather than imaging. During a stellar kinematic survey of the Galactic bulge, Ibata et al. (1994) noticed Sagittarius (Sgr) in color-velocity space as an excess of stars following a narrow velocity distribution offset from that of bulge members. Subsequent observations showed that Sgr, located just ~ 15 kpc behind the Galactic center, spews stars along tidal tails that wrap spectacularly around the entire sky (e.g., Mateo et al. 1996; Ibata et al. 1997; Majewski et al. 2003; Belokurov et al. 2006; Koposov et al. 2011a). The tidal disruption of Sgr provides a useful tracer of the Galactic potential (e.g., Johnston et al. 2005; Law & Majewski 2010; Peñarrubia et al. 2010), but disqualifies Sgr from a simple equilibrium-dynamical analysis. For this reason Sgr shall not be considered further here.

In a span of seven years, deep multi-color photometry from the Sloan Digital Sky Survey (SDSS) has now tripled the number of known Milky Way satellites (Willman et al. 2005b,a; Zucker et al. 2006b,a; Belokurov et al. 2006; Belokurov et al. 2007; Irwin et al. 2007; Walsh et al. 2007; Belokurov et al. 2008; Belokurov et al. 2009; Grillmair 2009; Watkins et al. 2009; Belokurov et al. 2010). The 17 satellites discovered with SDSS data have extended the floor of the observed galaxy luminosity function from $M_V \gtrsim -8$ to $M_V \gtrsim -2$ (bottom panel of Figure 1), such that some galaxies are less luminous than some stars! Unlike their brighter ‘classical’ siblings, the ‘ultrafaint’ satellites¹ discovered with SDSS data are not apparent to the eye, even in deep images. Rather, they are detected only by correlating spatial overdensities with overdensities in color-magnitude space (e.g., Belokurov et al. 2006; Walsh et al. 2009). In order to confirm the faintest satellites, the SDSS catalog must be supplemented by deeper, follow-up photometry as well as spectroscopy (e.g., Belokurov et al. 2009, 2010). Given the rate of false positives expected for candidates remaining in SDSS data ($\gtrsim 4/5$ in the author’s experience), the expense of follow-up observations can be prohibitive. However, the next generation of sky surveys (Pan-STARRS, SkyMapper, DES, Gaia, LSST, etc.) will almost certainly bring a new flurry of discoveries, particularly in the relatively unexplored southern sky.

Although they are not considered further below, it is worth noting that Shapley was correct regarding the dSph satellites of M31. van den Bergh (1972) discovered the first example with the Palomar Schmidt telescope, using plates more sensitive than those used in the original Palomar Survey. The current census includes 27 known dSph satellites of M31. Two-thirds of this number were discovered in the past seven years (Zucker et al. 2004; Martin et al. 2006; Ibata et al. 2007; Zucker et al. 2007; Majewski et al. 2007; Irwin et al. 2008; McConnachie et al. 2008; Martin et al. 2009; Richardson et al. 2011; Slater et al. 2011; Bell et al. 2011), with SDSS data as well as photometry from the PAndAS survey conducted with the Canada-France-Hawaii Telescope (McConnachie et al. 2009).

¹As Figure 1 and the terms themselves suggest, the distinction between ‘classical’ and ‘ultrafaint’ dSphs involves a mixture of intrinsic luminosity with sequence of discovery. Here this distinction (which is meaningless in the sense that members of both classes trace smooth scaling relationships involving luminosity, size, metallicity and stellar kinematics) is preserved only because observational studies of these objects—for both practical and accidental reasons—tend to be separable along the same lines. Following common practice, dSphs known before SDSS (Carina, Draco, Fornax, Leo I, Leo II, Sculptor, Sextans, Ursa Minor) are referred to as ‘classical’, and the rest as ‘ultrafaint’.

2.2. Stellar Structure

Galactic dynamics is concerned with the relationship between gravitational potential and the distribution of stars in phase space. Observers who study dark matter in dSph galaxies must gather information about the positions and velocities of dSph stars. The largest dSphs subtend solid angles of several square degrees, making it difficult to study their stellar structure at large radius. Complete homogenous surveys are rare and valuable.

2.2.1. ‘Classical’ dSphs

Hodge (1961b,a, 1962, 1963, 1964a,b) used photographic plates obtained at the Palomar (48-inch Schmidt, 100-inch and 200-inch), Lick (120-inch) and Boyden Station (24-inch Schmidt) in order to study luminous structure of the six Milky Way dSphs known at the time (Sculptor, Fornax, Leo I, Leo II, Draco and Ursa Minor). Hodge counted stars within squares of regular grids overlaid on each plate, and provides this description of analog data reduction: ‘Each plate was counted at one sitting so that uniformity would be maintained. The plates were counted to the limiting magnitude and each was counted once. From experience ... it was decided that the reproducibility of counts on a particular plate is greater than from plate to plate, so that it is better to count many plates each once than one plate many times’ (Hodge 1961b).

Figure 2 (top two rows of panels) displays isopleth maps that Hodge drew by connecting squares containing equal numbers of stars. These maps reveal that the internal structure of dSphs is smooth. Hodge reasoned that a well-mixed dSph requires dynamical relaxation by a process other than stellar encounters, as the low surface densities of dSphs imply internal relaxation timescales of $\gtrsim 10^3$ Hubble times. Hodge (1966) and Hodge & Michie (1969) would later suggest that encounters between stellar groups might enable exchanges of orbital energy over shorter timescales during dSph formation. Eventually Lynden-Bell (1967) would show that the time-varying gravitational potential of a young galaxy effectively shuffles the orbital energies of its stars, generating ‘violent’ relaxation without stellar encounters. More recently, Mayer et al. (2001b) have proposed a mechanism specific to dSphs, demonstrating with N-body/hydrodynamical simulations that repeated tidal encounters with the Milky Way can effectively transform a rotating dSph progenitor into a pressure-supported spheroid in less than a Hubble time.

Hodge discovered two other structural features common to the classical dSphs. First, most exhibit flattened morphology, with typical ellipticities of $\epsilon \equiv 1 - b/a \sim 0.3$, where a and b are semi-major and semi-minor axes, respectively. Second, dSph stellar density profiles decline more steeply at large radius than do the profiles of giant elliptical galaxies. Whereas the latter are commonly fit by formulae with relatively shallow outer profiles, e.g., $\Sigma(R) = \Sigma(0)/(1 + R/a)^2$ (Hubble 1930) or $\Sigma(R) = \Sigma(0)\exp[-kR^{1/4}]$ (de Vaucouleurs 1948), Hodge found that classical dSphs all have steeper

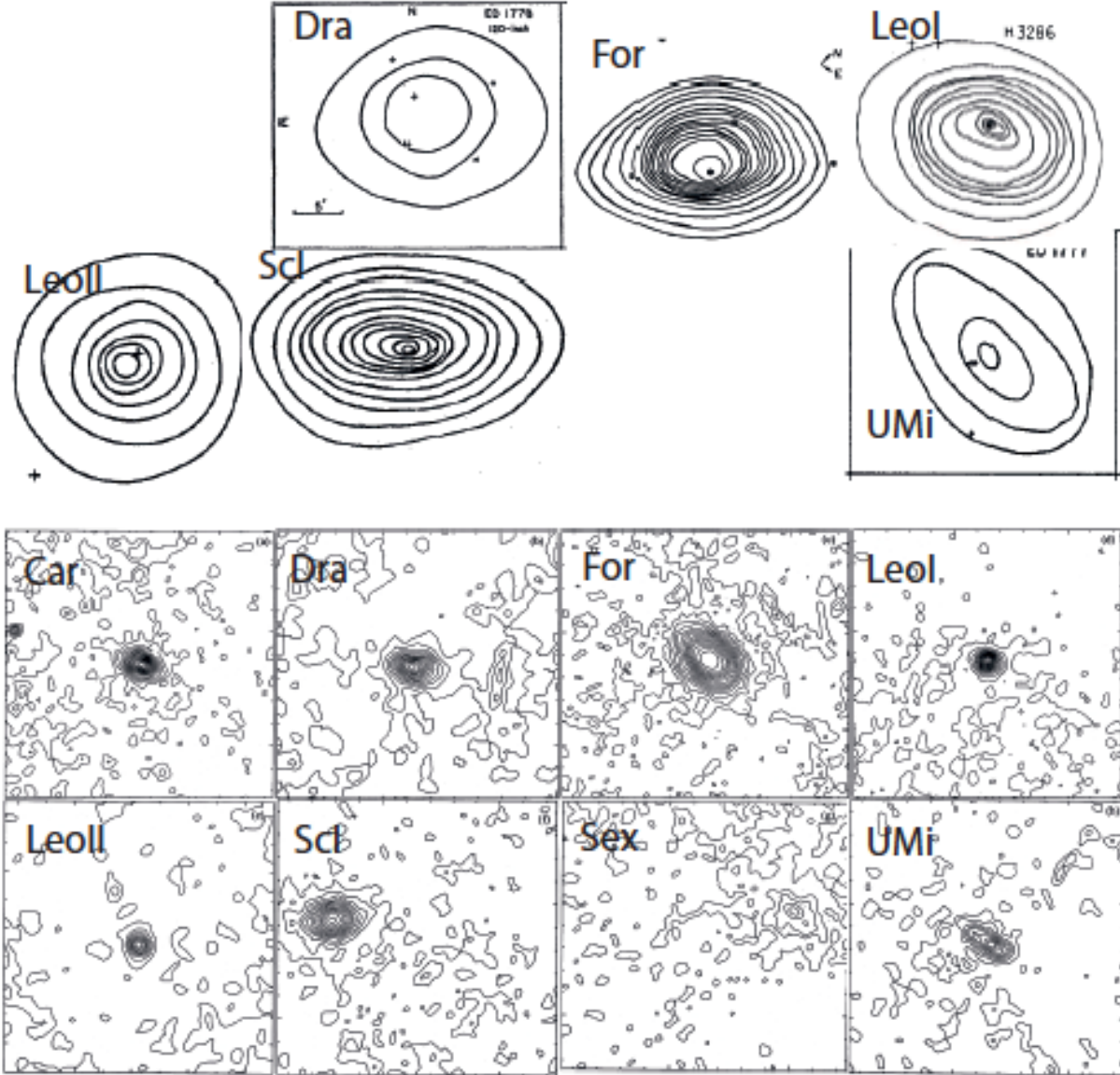


Fig. 2.— Stellar isodensity maps for the Milky Way’s eight ‘classical’ dSphs. *Top two rows*: from Hodge’s star count studies (Hodge 1961b,a, 1962, 1963, 1964a,b, reproduced by permission of the American Astronomical Society). *Bottom two rows*: reproduced from *Structural Parameters for the Galactic Dwarf Spheroidals*, by M. Irwin & D. Hatzidimitriou, MNRAS, 277, 1354, 1995 (by permission of John Wiley & Sons Ltd.).

outer profiles that are better fit with the formula of King (1962):

$$\Sigma(R) = k \left[\frac{1}{\sqrt{1+(R/R_c)^2}} - \frac{1}{\sqrt{1+(R_K/R_c)^2}} \right]^2, \quad (1)$$

where R_c is a ‘core’ radius and R_K is a maximum, or ‘limiting’ radius that one might expect to result from tidal truncation (Section 2.2.3)².

Three decades later, Irwin & Hatzidimitriou (1995, ‘IH95’ hereafter) used the APM facility at Cambridge to count stars automatically on photographic plates from the Palomar and UK Schmidt telescopes. While confirming Hodge’s findings, IH95 produced significantly deeper maps and were able to include Carina and Sextans, the two Milky Way dSphs discovered in the interim (Figure 2). IH95 used these maps to measure the centroid, ellipticity and orientation of each dSph, and then to tabulate stellar density as a function of distance along the semi-major axis. While the homogeneous analysis of IH95 continues to provide a valuable resource particularly for comparing dSphs in the context of scaling relations (Section 5), deeper photometric data sets now exist for most of the classical dSphs (e.g., Stetson et al. 1998; Majewski et al. 2000; Saviane et al. 2000; Odenkirchen et al. 2001; Palma et al. 2003; Walcher et al. 2003; Lee et al. 2003; Tolstoy et al. 2004; Coleman et al. 2005a,b; Battaglia et al. 2006; Westfall et al. 2006).

In principle the structure of dSph stellar components carries information about the mechanisms that drive dSph formation and evolution. While incompatible with shallow Hubble and de Vaucouleurs profiles, the available data often do not distinguish the King profile (Equation 1) from other commonly adopted fitting formulae—e.g., exponential and Plummer (1911) profiles,

$$\Sigma(R) = \Sigma(0) \exp[-R/R_e] \quad (2)$$

and

$$\Sigma(R) = \frac{\Sigma(0)}{[1+(R/R_h)^2]^2}, \quad (3)$$

respectively, where $R_h \approx 1.68R_e$ is the projected half-light radius (i.e., the radius of the circle enclosing half the stars as viewed in projection). Figure 3 displays IH95’s fits of King (1966) and exponential surface brightness profiles to the Milky Way’s classical dSph satellites.

2.2.2. Ultrafaint dSphs

The SDSS catalog enables homogeneous studies of the structural properties of ultrafaint dSphs. For example, Figure 4 displays isopleth maps constructed by Belokurov et al. (2007) for

²In fact R_K is usually referred to as a ‘tidal’ radius and denoted r_t . The adopted nomenclature and notation avoid confusion with the tidal radius defined in Equation 4.

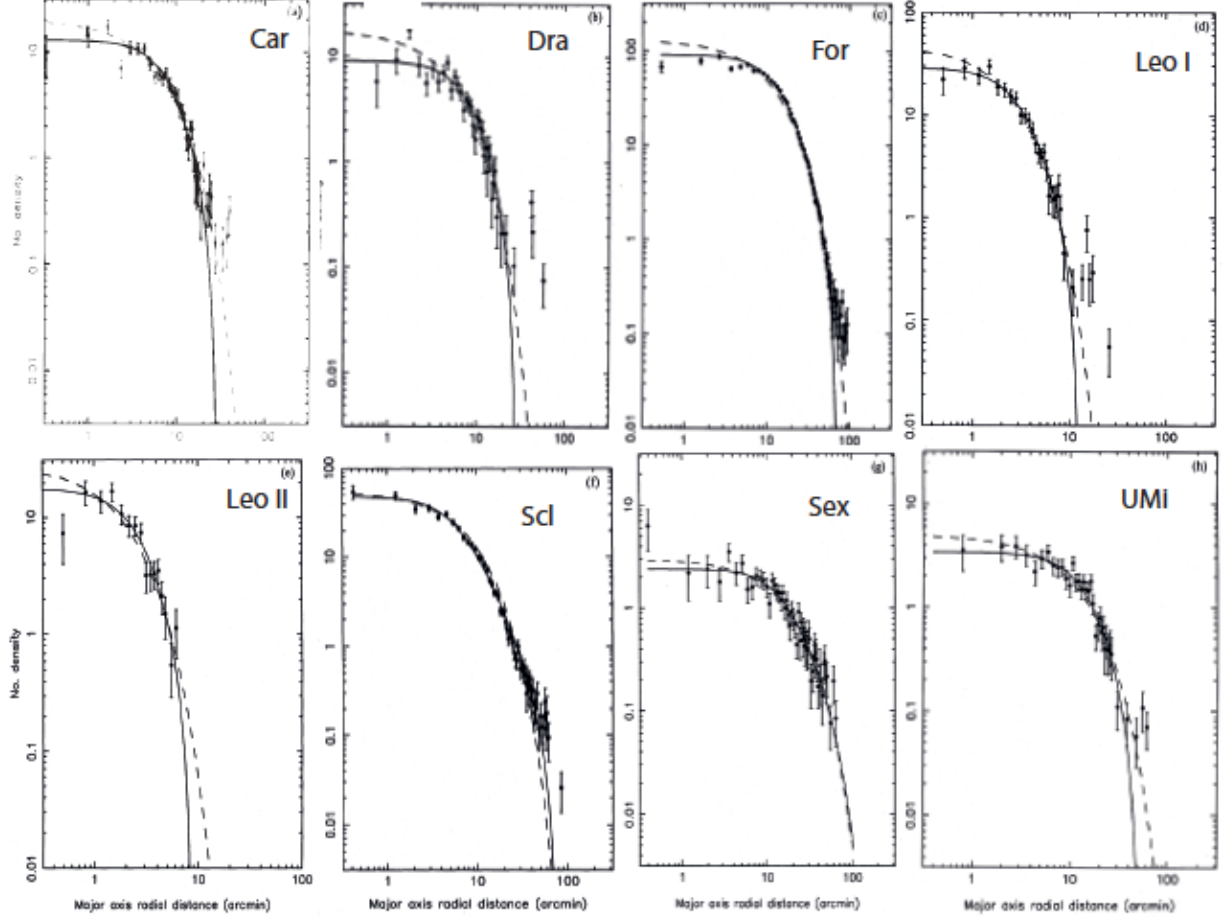


Fig. 3.— Stellar density profiles for the Milky Way’s ‘classical’ dSphs. Overlaid are best-fitting King (1966, solid) and exponential (dashed) surface brightness profiles. Reproduced from *Structural Parameters for the Galactic Dwarf Spheroidals*, by M. Irwin & D. Hatzidimitriou, MNRAS, 277, 1354, 1995 (by permission of John Wiley & Sons Ltd.).

Coma Berenices, Canes Venatici II, Segue 1 and Hercules using both SDSS and deeper follow-up data. Whereas Hodge and IH95 estimated structural parameters for the classical dSphs after binning their star-count data and subtracting estimates of foreground densities, the low surface brightnesses of ‘ultrafaint’ dSphs are conducive neither to binning nor to foreground subtraction. Fortunately, neither procedure is necessary; indeed Kleyna et al. (1998) estimate structural parameters for the classical dSph Ursa Minor using a likelihood function that specifies the probability associated with each individual stellar position in terms of a parametric surface brightness profile plus constant foreground.

Martin et al. (2008) design a similar maximum-likelihood analysis that operates directly on unbinned SDSS data in order to estimate the centroid, half-light radius, luminosity, ellipticity and orientation of each ultrafaint satellite. Figure 5 demonstrates the efficacy of their method. The left panel maps individual stars from the SDSS catalog that are near the line of sight to Boötes I and satisfy color/magnitude criteria designed to select red giants at the distance of Boötes I. Panels on the right-hand side show maximum-likelihood estimates of each free parameter. Marginalised error distributions include the effects of sampling errors and parameter covariances, and can be used directly in subsequent kinematic/dynamical analyses (Section 4).

Martin et al. (2008) show that their method recovers robust estimates even when the SDSS sample includes as few as tens of satellite members. Subsequent tests with synthetic data by Muñoz et al. (2011) provide reason for caution, suggesting that for objects with low surface brightness, insufficient contrast between members and foreground can generate biased estimates of structural parameters. It is reassuring that deeper observations with CFHT (Muñoz et al. 2010) and Subaru (Okamoto et al. 2012) yield structural parameters for subsets of ultrafaint satellites that agree well with the SDSS-derived estimates of Martin et al. (2008).

2.2.3. *Extended Structure*

The outer stellar structure of a given dSph is determined by some combination of formation processes and subsequent evolution within the external potential of the Milky Way. In his structural analyses of the six dSphs known in the 1960s, Hodge compared the observed limiting radii, R_K (Equation 1), to simple estimates of ‘tidal’ radii, r_t , beyond which stars escape into the external potential of the Milky Way (von Hoerner 1957; King 1966):

$$r_t = R_D \left[\frac{M_D}{(3+e)M_{MW}} \right]^{1/3}. \quad (4)$$

Here, M_{MW} and M_D are the Milky Way and dSph (point) masses, respectively, R_D is the pericentric distance of the dSph’s orbit and e is orbital eccentricity. Assuming circular orbits and considering only luminous masses, Hodge (1966) noticed that while the two radii are similar for the nearest dSphs (Draco, Sculptor, Ursa Minor), for the three most distant dSphs (Leo I, Leo II, Fornax), $R_K \lesssim 0.5r_t$. Hodge (1966) concluded that tidal forces play a significant role in shaping the outer

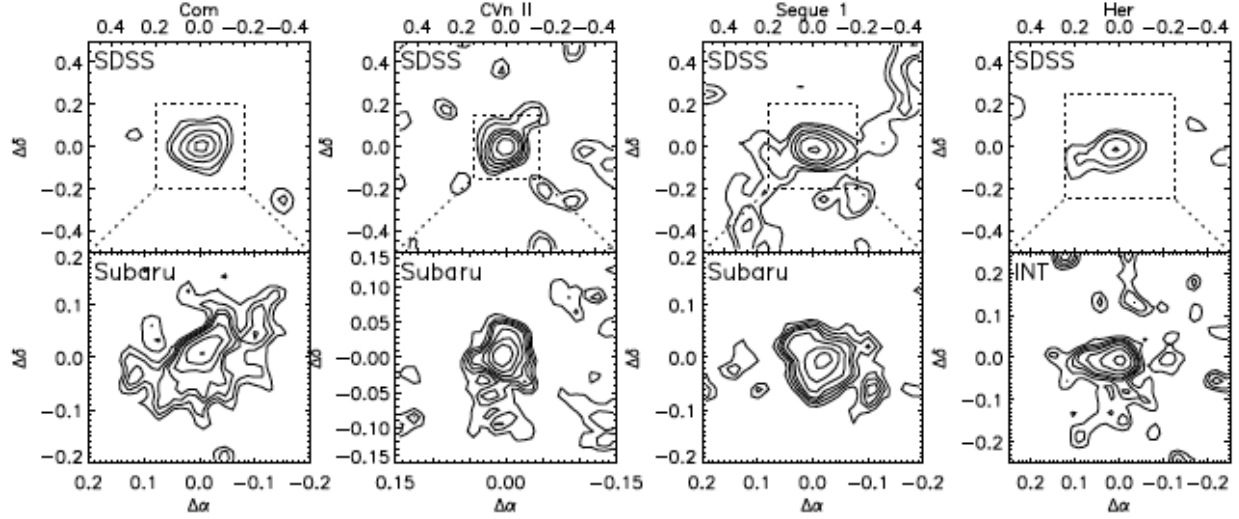


Fig. 4.— Stellar isodensity maps for four of the Milky Way’s ‘ultrafaint’ dSphs, from the discovery paper of Belokurov et al. (2007, reproduced by permission of the American Astronomical Society).

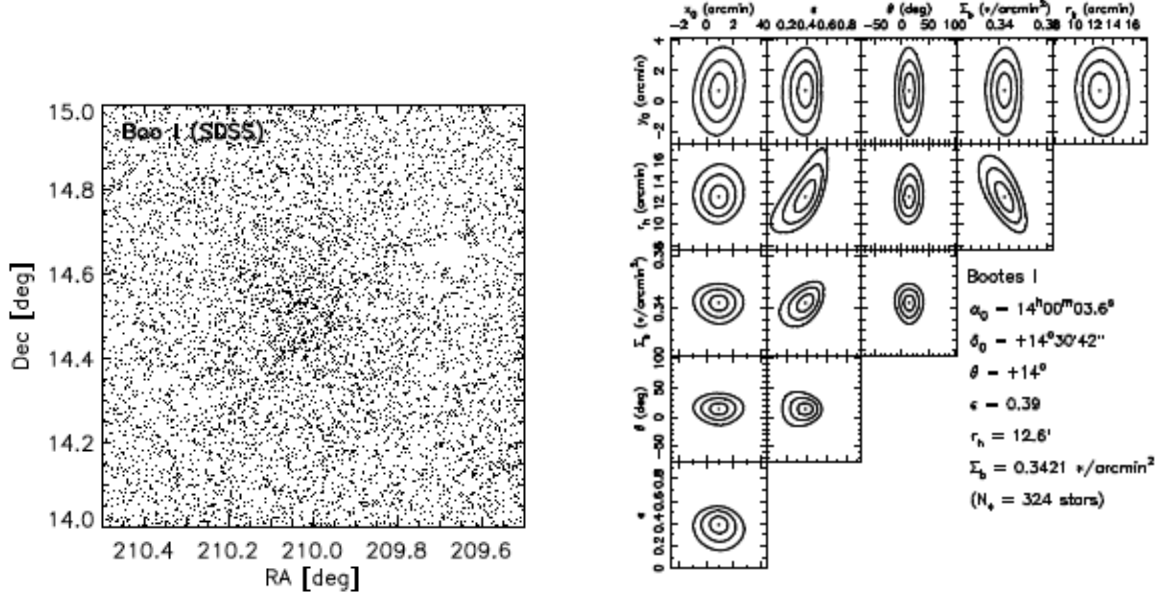


Fig. 5.— Measurement of structural parameters for the Boötes I dSph from SDSS data (Martin et al. 2008). *Left*: sky positions of red giant candidates selected from the SDSS catalog. *Right*: constraints on structural parameters, from the maximum-likelihood analysis of Martin et al. (2008, reproduced by permission of the American Astronomical Society).

structures of the nearest dSphs.

Low surface brightness in the outer regions of dSphs makes extended structural studies difficult to conduct and interpret. For example, Coleman et al. (2005a) use deep wide-field photometry to conclude that Sculptor’s surface brightness profile is well described as the superposition of two equilibrium stellar components with different scale radii. Using an independent data set, Westfall et al. (2006) fit a single profile and identify a ‘break’ in Sculptor’s surface brightness profile, which makes an apparent transition from a King profile in the inner parts to a shallower power law in the outer parts. Westfall et al. (2006) cite this transition not as evidence for a second component, but rather as a signal that Sculptor is losing stars to tidal disruption.

In many cases, the use of narrow-band filters that are sensitive to stellar surface gravity (e.g., DDO51) can help to distinguish dSph red giants from foreground dwarf stars, providing a valuable boost in contrast (e.g., Majewski et al. 2000, 2005; Palma et al. 2003; Westfall et al. 2006). Having used narrow-band photometry to select spectroscopic targets at large dSph radii, Muñoz et al. (2005) and Muñoz et al. (2006) present velocities that confirm the membership of stars in Ursa Minor and Carina (Figure 6) out to radii ~ 3 and ~ 5 times larger, respectively, than estimates of R_K . These detections imply that tides can play a significant role in shaping the outer parts of dSphs (Section 3.2).

2.2.4. *Structural Peculiarities of Individual dSphs*

Most kinematic analyses of dSphs proceed from the assumption that dSphs host a single, spherically symmetric stellar component in dynamic equilibrium (Section 4). However, real dSphs are all flattened ($0.1 \lesssim \epsilon \equiv 1 - b/a \lesssim 0.7$, Irwin & Hatzidimitriou 1995; Martin et al. 2008; Sand et al. 2011), and it is not clear how severely this violation of spherical symmetry affects conclusions regarding dSph dynamics. In fact most dSphs exhibit individual peculiarities that further violate the simplistic assumptions (Section 4) employed in kinematic analyses.

For example, Sculptor, Fornax and Sextans all display evidence for chemo-dynamically independent stellar *sub*-populations (Tolstoy et al. 2004; Battaglia et al. 2006; Battaglia et al. 2011, respectively). In all three cases, a relatively metal-rich, kinematically cold population has smaller scale radius than does a metal-poor, kinematically hot population (Section 4.2.2, Figure 10). Fornax also has irregular stellar structure in the form of a crescent-shaped feature near its center (Stetson et al. 1998, and Figure 7, left panel), two shell-like features (Coleman et al. 2004) and lobes along its morphological minor axis (Coleman et al. 2005b, and Figure 7, right panel). These features suggest that Fornax may have undergone a recent merger, an event that might be related to the presence of a young (age ~ 100 Myr), centrally concentrated main sequence in Fornax (Battaglia et al. 2006). Ursa Minor exhibits clumpy stellar substructure, most dramatically in the form of a secondary peak in its luminosity distribution, offset by $\sim 20'$ from the central peak (Olszewski & Aaronson 1985). The region near the secondary peak is kinematically colder than the rest of Ursa Minor (Kleyna et al. 2003), and so may represent a bound star cluster (Section 4.2.1).

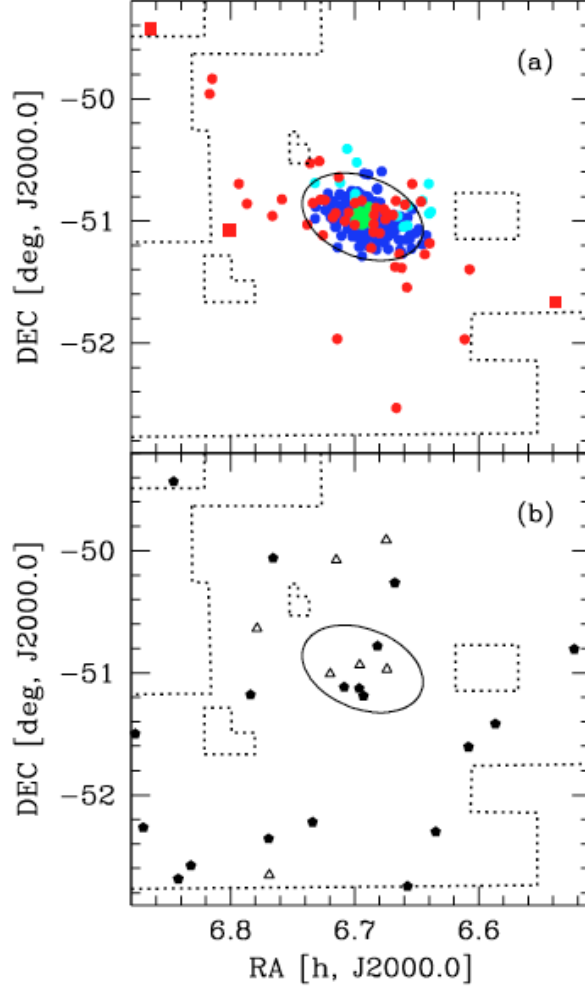


Fig. 6.— Extended stellar structure of the Carina dSph, from narrow-band photometry and spectroscopy of Muñoz et al. (2006, reproduced by permission of the American Astronomical Society). The top/bottom panels show sky positions of red giant candidates confirmed as Carina members/nonmembers. Ellipses mark Carina’s limiting radius, R_K (Equation 1), determined from smooth fits to star count data. The extension of faint stellar structure at $R \gtrsim 3R_K$ suggests tidal interaction (Section 3.2). Muñoz et al. (2005) report similar results for Ursa Minor.

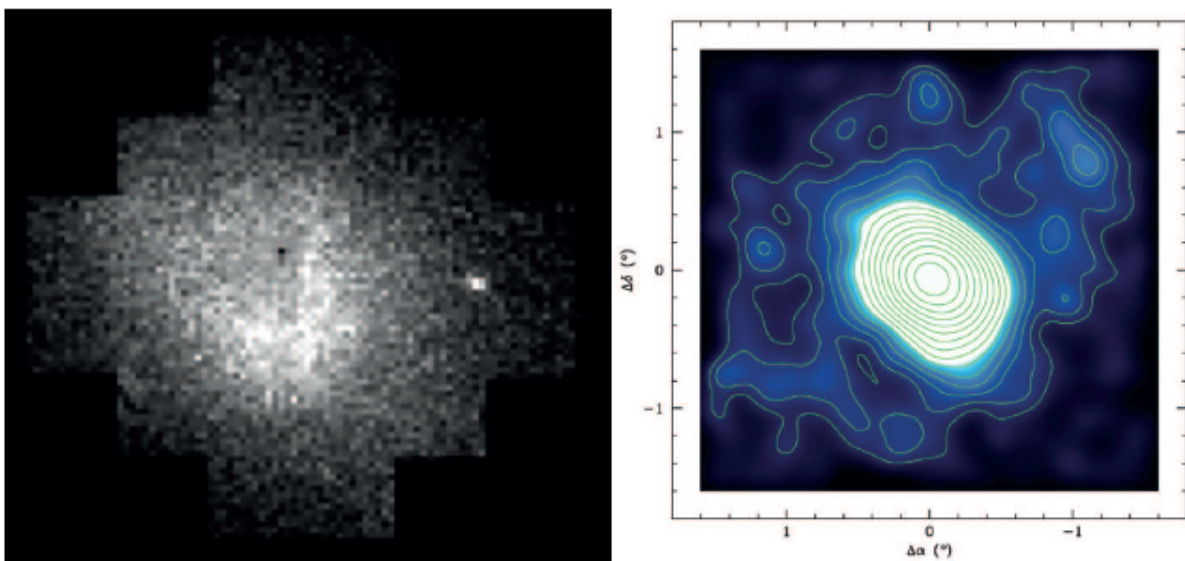


Fig. 7.— Structural irregularities in Fornax. *Left:* Grayscale map ($\sim 42'$ per side) of surface density of stars with $18.5 \leq V \leq 23$, from the photometry of Stetson et al. (1998, reproduced with permission from The University of Chicago Press). Notice the crescent-like feature near the center. *Right:* Smoothed stellar map from V, I photometry of Coleman et al. (2005b, reproduced by permission of the American Astronomical Society), who detect two shell-like features (one is visible ~ 1.3 deg northwest of the center) aligned with lobes along the morphological minor axis.

Such peculiarities extend to the ultrafaint satellites as well. Spectroscopic surveys reveal that Segue 1 is superimposed on at least one stream of stellar debris (Geha et al. 2009; Niederste-Ostholt et al. 2009; Simon et al. 2011), offset by $\sim 100 \text{ km s}^{-1}$ from Segue 1 in velocity space. Segue 1 also shows hints of extended stellar structure superimposed on Sgr debris, although interpretation of these extremely low-surface-brightness features in terms of tidal disruption remains controversial (Belokurov et al. 2007; Geha et al. 2009; Niederste-Ostholt et al. 2009; Simon et al. 2011). Segue 2 appears to be embedded in—and comoving with—a stream of stellar debris, perhaps from a tidally disrupted parent system (Belokurov et al. 2009). Ursa Major II has flattened morphology and distorted outer morphology that suggest ongoing tidal disruption (Zucker et al. 2006a; Muñoz et al. 2010). Another strong candidate for disruption is Boötes III, which has irregular, clumpy morphology and a large measured velocity dispersion of $\sigma \sim 14 \text{ km s}^{-1}$ (Carlin et al. 2009). The alignment of stellar distortions in Leo IV and Leo V hints at a low surface brightness ‘bridge’ spanning the $\sim 20 \text{ kpc}$ between these systems (Belokurov et al. 2008; Walker et al. 2009a; de Jong et al. 2010; note, however, that Sand et al. 2010 detect no such feature in deep photometry around Leo IV). Stars nearest the center of the Willman 1 satellite exhibit near-zero velocity dispersion and a mean velocity that is offset from the rest of Willman 1 members by $\sim 8 \text{ km s}^{-1}$ (Willman et al. 2011). Each newly discovered galaxy seems to present a new quirk of its own.

2.3. Stellar Velocities

Assuming that dSphs are purely stellar systems truncated by tidal interaction with the Milky Way, such that $r_t \sim R_K$, Ostriker et al. (1974) applied Equation 4 to estimate the mass of the Milky Way. Inverting the calculation by assuming an isothermal Galactic halo with $v_{\text{circ}} = 225 \text{ km s}^{-1}$, Faber & Lin (1983) estimated masses of dSphs. For the nearest dSphs (Draco, Ursa Minor, Carina, Sculptor), Faber & Lin estimated mass-to-light ratios of $M/L_V \gtrsim 10[M/L_V]_{\odot}$, suggesting dSph dark matter. Faber & Lin further used their estimates to predict, via the virial theorem, values of $\gtrsim 10 \text{ km s}^{-1}$ for the internal stellar velocity dispersions of dSphs.

At the same time, Aaronson (1983) provided the first actual measurement of a dSph’s internal velocity dispersion. Aaronson used the Multiple Mirror Telescope (MMT, which then consisted of six 1.8-meter mirrors working in tandem) to acquire high-resolution ($R \sim 30000$) spectra for three individual carbon stars in Draco. Figure 8 displays the spectra, which were sufficient for Aaronson to measure precise line-of-sight velocities of $-298.7 \pm 0.9 \text{ km s}^{-1}$ (with a follow-up measurement of $-297.6 \pm 0.6 \text{ km s}^{-1}$), $-300.2 \pm 0.6 \text{ km s}^{-1}$, and -279.7 km s^{-1} . Aaronson calculated that such measurements require, at the 95% confidence level, an intrinsic velocity dispersion of $\sigma \gtrsim 6.5 \text{ km s}^{-1}$.³ From dynamical arguments based on the virial theorem (Illingworth 1976; Richstone & Tremaine 1986, Section 4.1.1), such a large dispersion indicates a large dynamical mass-to-light

³Aaronson added to the final article proof a measurement of $-285.6 \pm 1.1 \text{ km s}^{-1}$ for a fourth, non-carbon star, further supporting a large dispersion.

ratio $M/L_V \gtrsim 30[M/L_V]_\odot$, confirming the prediction of Faber & Lin (1983) and indicating the presence of dark matter.

Figure 9 plots the number of stars observed in dSph stellar velocity surveys as a function of time. The three decades of observations separate neatly into ‘epochs’ defined by the available instrumentation.

2.3.1. *Small-Number Statistics*

The 1980s yielded the first precise velocity measurements for individual stars in Draco (Aaronson 1983), Carina, Sculptor, and Fornax (Seitzer & Frogel 1985), Leo I and Leo II (Suntzeff et al. 1986) and Ursa Minor (Aaronson & Olszewski 1987a), and follow-up observations of Sculptor (Armandroff & Da Costa 1986) and Draco (Aaronson & Olszewski 1987b). These samples typically included $\lesssim 10$ stars per galaxy and indicated velocity dispersions of $\sigma \sim 6–10 \text{ km s}^{-1}$, suggesting that dSph dynamical mass-to-light ratios reach at least double the values estimated for globular clusters. Strong implications for the particle nature of dark matter (Tremaine & Gunn 1979; Lin & Faber 1983, Section 6.2) drew immediate attention. Nevertheless, skepticism regarding small samples, velocity precision and the unknown contribution of binary orbital motions to the measured velocity dispersions demanded further observations and better statistics.

2.3.2. *Confirmation*

In the 1990s, several groups accumulated velocity samples for tens of stars per dSph. Including Aaronson’s original work, nine seasons of observations with the MMT eventually produced velocity samples that reached ~ 20 members in each of the Draco and Ursa Minor dSphs (Olszewski et al. 1995; Armandroff et al. 1995), yielding velocity dispersion measurements of $\sigma \sim 10 \text{ km s}^{-1}$ and dynamical mass-to-light ratios $M/L_V \sim 75[M/L_V]_\odot$ for both galaxies. Meanwhile, medium-resolution ($R \sim 12000$) spectra from the William Herschel Telescope gave velocity samples for tens of stars in each of Draco, Ursa Minor and the newly discovered Sextans (Hargreaves et al. 1994b,a, 1996b). High-resolution spectra from ESO’s 3.6-m and NTT telescopes (Queloz et al. 1995) and Keck/HIRES (Mateo et al. 1998) delivered precise velocities for 23 and 33 stars in Sculptor and Leo I, respectively. In all cases, velocity dispersions of $\sigma \gtrsim 6 \text{ km s}^{-1}$ indicated $M/L_V \gtrsim 10[M/L_V]_\odot$.

Providing an early demonstration of the efficiency of multi-object fiber spectroscopy, Armandroff et al. (1995) compiled samples of ~ 100 velocities in each of Draco and Ursa Minor using the HYDRA multi-fiber spectrograph at the KPNO 4-meter telescope. This data set included many repeat measurements, which Olszewski et al. (1996) used to estimate a binary fraction of $\sim 0.2–0.3$ for periods of ~ 1 year. Based on Monte Carlo simulations, Olszewski et al. (1996) and Hargreaves et al. (1996a) concluded that binary motions contribute negligibly to the velocity

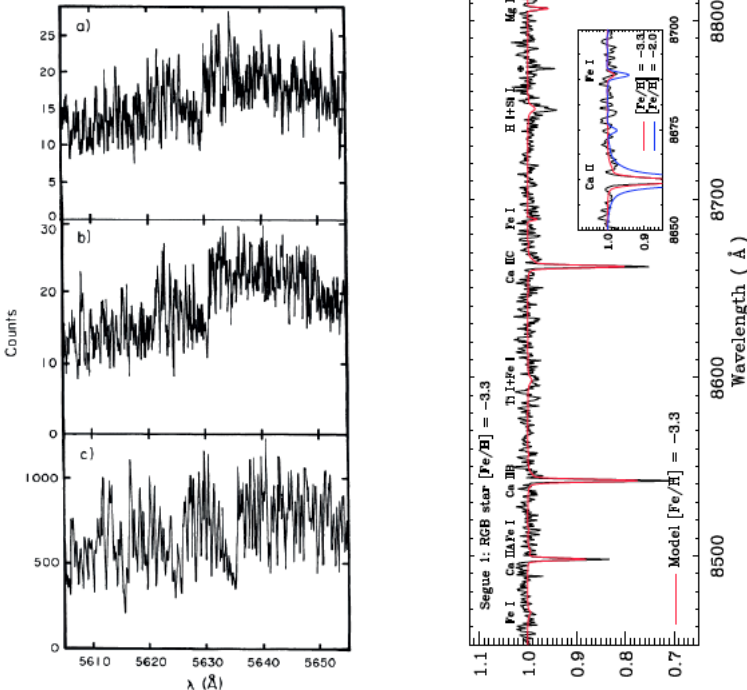


Fig. 8.— Examples of spectra for individual dSph stars. *Left*: MMT echelle spectra ($R \sim 30000$) for three carbon stars in Draco, used for the first measurement of a dSph velocity dispersion (Aaronson 1983, reproduced by permission of the American Astronomical Society). *Right*: Keck/DEIMOS spectrum ($R \sim 6000$) for the brightest red giant in Segue 1 (Geha et al. 2009, reproduced by permission of the American Astronomical Society), with absorption features labeled and best-fitting model overplotted.

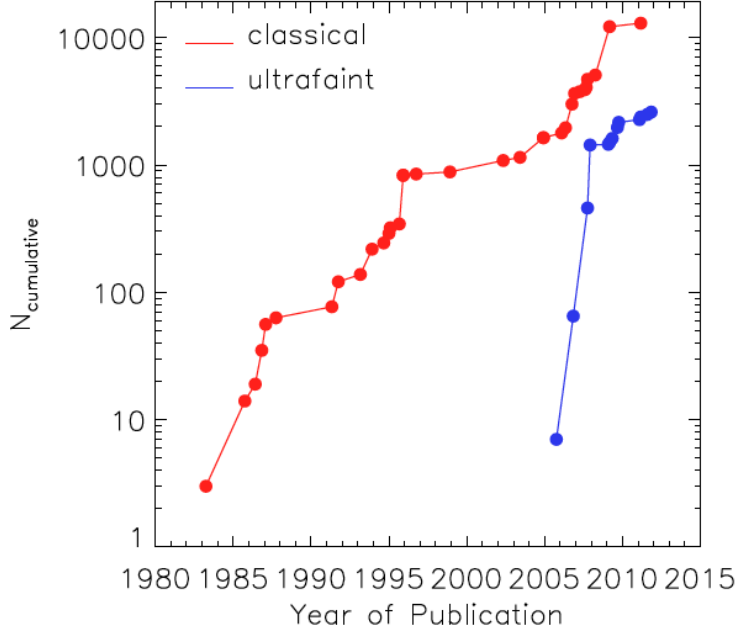


Fig. 9.— Growth of sample sizes available for internal kinematic studies of the Milky Way’s dSph satellites. Plotted as a function of time is the cumulative number of line-of-sight velocities measured for individual stars (including foreground contamination) targeted in dSph spectroscopic surveys. References: Aaronson (1983); Seitzer & Frogel (1985); Suntzeff et al. (1986); Armandroff & Da Costa (1986); Aaronson & Olszewski (1987b,a); Mateo et al. (1991); Da Costa et al. (1991); Suntzeff et al. (1993); Mateo et al. (1993); Hargreaves et al. (1994b,a); Armandroff et al. (1995); Vogt et al. (1995); Queloz et al. (1995); Olszewski et al. (1995); Hargreaves et al. (1996b); Mateo et al. (1998); Kleyna et al. (2002, 2003); Tolstoy et al. (2004); Kleyna et al. (2005); Muñoz et al. (2006); Muñoz et al. (2006); Battaglia et al. (2006); Westfall et al. (2006); Walker et al. (2006, 2007a); Koch et al. (2007b,a); Martin et al. (2007); Simon & Geha (2007); Sohn et al. (2007); Mateo et al. (2008); Koch et al. (2009); Geha et al. (2009); Walker, Mateo & Olszewski (2009); Walker et al. (2009a); Belokurov et al. (2009); Carlin et al. (2009); Willman et al. (2011); Simon et al. (2011); Adén et al. (2011); Koposov et al. (2011b); Battaglia et al. (2011).

dispersions measured for classical dSphs (Section 3.3).

In the southern hemisphere, Mateo et al. (1991) used Las Campanas Observatory’s 2.5-meter telescope and ‘2D Frutti’ echelle photon counter to measure velocities for 44 Fornax stars, including an outer field that showed the same velocity dispersion ($\sigma \sim 10 \text{ km s}^{-1}$) as the central stars, indicating $M/L_V \sim 10[M/L_V]_{\odot}$. After measuring a velocity dispersion of $\sigma \sim 7 \text{ km s}^{-1}$ and $M/L_V \sim 40[M/L_V]_{\odot}$ from the velocities of 17 Carina stars, Mateo et al. (1993) noted a scaling relation among dSphs: the dynamical mass-to-light ratios of classical dSphs are inversely proportional to luminosity, suggesting similar dynamical masses of $\sim 10^7 M_{\odot}$ (Section 5).

2.3.3. *Large Samples*

The gap in Figure 9 between 1998–2002 signifies a period not of inactivity but rather of construction. During this time, wide-field multi-object spectrographs were built for the world’s largest telescopes. Over the past decade, surveys with these new instruments have increased stellar velocity samples from tens to thousands per dSph. Kleyna et al. (2002, 2003, 2004) used the Wide-Field Fibre Optic Spectrograph (WYFFOS) at the 2.5-meter Isaac Newton Telescope to measure velocities for ~ 100 stars in each of Draco, Ursa Minor and Sextans, respectively. These samples were sufficiently large to examine the velocity distribution as a function of distance from the dSph center (e.g., Wilkinson et al. 2002; Kleyna et al. 2002, 2004; Wilkinson et al. 2004; Section 4).

Soon thereafter, the Dwarf Abundances and Radial Velocities Team (DART) used the FLAMES fiber spectrograph at the 8.2-meter Very Large Telescope (VLT; UT2) to measure velocities and metallicities (derived from the strength of the calcium-triplet absorption feature at $\sim 8500 \text{ \AA}$) for ~ 310 , ~ 560 and ~ 175 members of Sculptor, Fornax and Sextans, respectively (Tolstoy et al. 2004; Battaglia et al. 2006; Battaglia et al. 2011). These samples yielded the discovery that all three of these dSphs contain multiple, chemodynamically independent stellar populations (Figure 10 and Section 4.2.2). Also with VLT/FLAMES, Koch et al. (2007a) measured a velocity dispersion of $\sigma \sim 7 \text{ km s}^{-1}$ from ~ 170 members of Leo II, providing what remains the largest published sample for this galaxy.

Meanwhile Muñoz et al. (2006) used archival VLT/FLAMES spectra (see also Fabrizio et al. 2011) to measure velocities for ~ 300 Carina members and added another ~ 45 members from spectra obtained sequentially with the MIKE spectrograph at the Magellan/Clay 6.5-meter telescope. The extra members observed with MIKE extend to ~ 5 times Carina’s limiting radius as determined from photometry (Figure 6), indicating that Carina has lost mass to tidal interactions with the Milky Way.

Koch et al. (2007a) used a pair of multi-slit spectrographs—the Gemini Multiobject Spectrograph (GMOS) at the Gemini-North 8-meter telescope and the Deep Imaging Multi-object Spectrograph (DEIMOS) at the Keck 10-meter telescope—to measure velocities for ~ 100 members of Leo I. Sohn et al. (2007) added another ~ 100 members from their own observations with

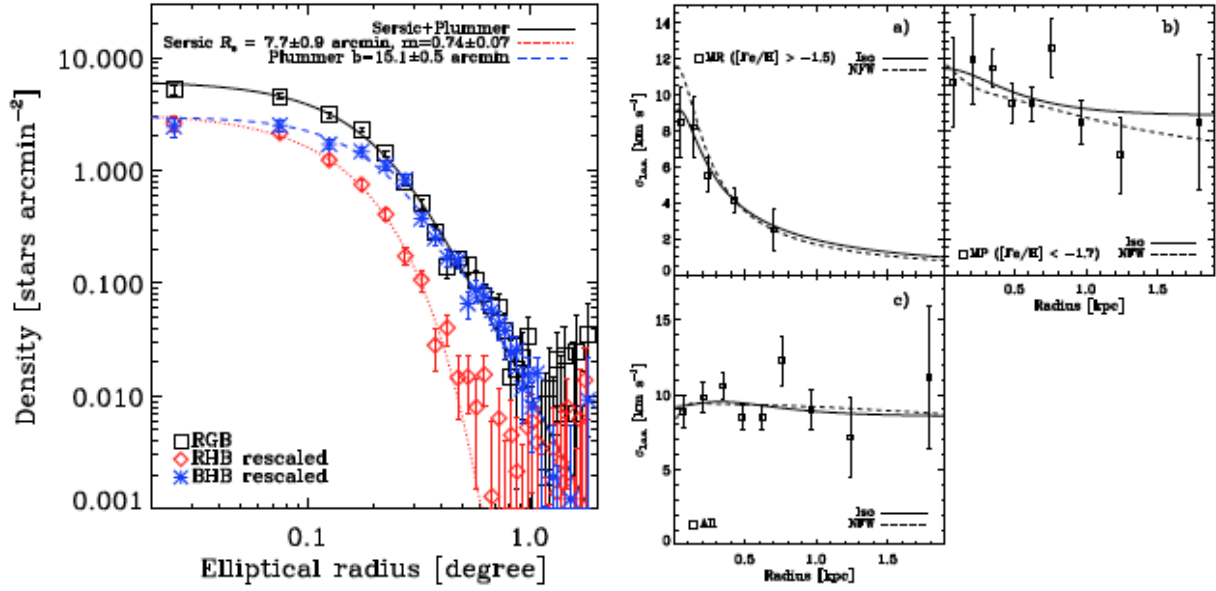


Fig. 10.— Sculptor’s two chemodynamically independent stellar sub-populations (Battaglia et al. 2008, reproduced by permission of the American Astronomical Society ; see also Tolstoy et al. 2004). *Left*: Surface brightness profiles for Sculptor’s red giants (black), red-horizontal branch (red) and blue-horizontal branch stars. *Right*: Velocity dispersion profiles, calculated for subsets of relatively metal-rich (top left) and metal-poor (top right), as determined from the VLT/FLAMES spectroscopic sample of Tolstoy et al. (2004). For comparison, the lower-left panel plots the velocity dispersion profile measured from the composite population.

Keck/DEIMOS, and Mateo et al. (2008) contributed velocities for ~ 300 Leo I members using the Hectochelle multi-fiber spectrograph at the MMT. The latter two studies explored larger radii and both found kinematic evidence for tidal streaming motions in the outskirts of Leo I. This result is surprising given Leo I’s current distance of ~ 250 kpc (Irwin & Hatzidimitriou 1995), leading Mateo et al. (2008) to suggest that Leo I’s orbit is nearly radial.

Operating from 2004–2011, the Michigan-MIKE Fiber Spectrograph (MMFS; $R \sim 20000$), built by Mario Mateo for the Magellan/Clay 6.5-meter telescope, provided what remain the largest homogeneous velocity samples for ‘classical’ dSphs. The public catalog of Magellan/MMFS velocities includes ~ 775 , ~ 2500 , ~ 1365 and ~ 440 members of Carina, Fornax, Sculptor and Sextans, respectively (Walker, Mateo & Olszewski 2009). Figure 11 displays the Fornax data, including sky positions as well as the two quantities measured from each spectrum: line-of-sight velocity and a spectral index that indicates the pseudo-equivalent width of the Mg-triplet feature at ~ 5170 Å. Data from a similar survey conducted in the North with MMT/Hectochelle will soon become public. Figure 12 displays velocity dispersion profiles calculated from the Magellan/MMFS and MMT/Hectochelle data, demonstrating that the luminous regions of classical dSphs have approximately constant velocity dispersion.

2.3.4. (Necessarily) Small Samples

With kinematic samples for ‘classical’ dSphs growing exponentially, discoveries of ‘ultra-faint’ dSphs with SDSS data generated a wave of interest in the faintest Milky Way satellites, and efforts to obtain spectroscopic follow-up began immediately. Kleyna et al. (2005) contributed a first result echoing Aaronson’s original study of Draco: from Keck/HIRES velocities for 5 members of Ursa Major I, Kleyna et al. (2005) estimate that $\sigma > 6.5$ km s $^{-1}$ with 95% confidence. Given UMaI’s low luminosity, simple dynamical models imply $M/L_V \gtrsim 500[M/L_V]_{\odot}$. Muñoz et al. (2006) used the HYDRA multi-fiber spectrograph at the 3.5-meter WIYN telescope to measure velocities for 7 members of the Boötes I dSph, obtaining a velocity dispersion of ~ 6.5 km s $^{-1}$ and $M/L_V \gtrsim 130[M/L_V]_{\odot}$.

Whereas spectroscopic surveys of ‘classical’ dSphs target bright red giant branch (RGB) stars, the least luminous ‘ultrafaint’ satellites host few RGBs. Samples for even tens of stars for such objects require observations of faint stars near the main sequence turnoff and are feasible only with the largest telescopes. Martin et al. (2007) and Simon & Geha (2007) used Keck/DEIMOS to observe tens of velocities in 10 of the 11 ‘ultrafaints’ known at the time, measuring $\sigma \gtrsim 3$ km s $^{-1}$ and concluding that these objects indeed have extremely large dynamical mass-to-light ratios, of order $M/L_V \gtrsim 100[M/L_V]_{\odot}$ and larger. Geha et al. (2009, see example spectrum in the right panel of Figure 8) and Simon et al. (2011) followed with a Keck/DEIMOS survey of Segue 1, measuring $\sigma \sim 4$ km s $^{-1}$ and concluding that this object is the ‘darkest galaxy’, with $M/L_V \sim 3400[M/L_V]_{\odot}$.

Adén et al. (2009) and Koposov et al. (2011b) used VLT/FLAMES to measure velocity dispersions for Hercules and Boötes I, respectively, that while indicative of large dynamical mass-to-light

ratios, are both smaller than previously measured with Keck/DEIMOS. Adén et al. (2009) obtained a smaller velocity dispersion after using Strömgren photometric criteria to remove foreground interlopers. Koposov et al. (2011b) used a novel observing strategy that included ~ 15 individual 45-60 minute exposures taken over a month. After measuring velocities for each exposure, Koposov et al. (2011b) were able to resolve binary orbital motions directly and to exclude stars that showed significant velocity variability (Section 3.3).

2.4. The Smallest Galaxies

Figure 13 displays two scaling relations defined by the structural and kinematic observations discussed above, and lets one compare the properties of objects classified as dSphs directly with those of objects classified as globular clusters. Parameters for globular clusters are adopted from the catalog of Harris (1996, 2010 edition).

The left-hand panel of Figure 13 plots luminosity against size, characterised by the projected half-light radius (Belokurov et al. 2007; Gilmore et al. 2007; Martin et al. 2008; Sand et al. 2011). Here one can appreciate another conclusion of Shapley’s (1938b) regarding the first known dSphs: ‘The Sculptor and Fornax systems might be called greatly expanded giant clusters’. Indeed, while the luminosity distributions of dSphs and globular clusters overlap substantially, most dSphs have $R_h \gtrsim 100$ pc while most globular clusters have $R_h \lesssim 10$ pc (Gilmore et al. 2007).⁴ The region between $10 \lesssim R_h/\text{pc} \lesssim 100$ is populated only by globular clusters with $M_V \lesssim -4$ or by dSphs with $M_V \gtrsim -4$.

Current kinematic results suggest that this separation in luminosity between the smallest dSphs and the largest globular clusters is not merely an artifact of classification, but points to a fundamental structural difference. The right-hand panel of Figure 13 plots the product $R_h \sigma^2 / (L_V G)$ (dimensionally a mass-to-light ratio) against luminosity. In the region of overlapping size, the less luminous objects tend to have larger velocity dispersions, amplifying the separation in luminosity such the smallest, faintest dSphs have the largest dynamical mass-to-light ratios of any known galaxies (Kleyna et al. 2005; Muñoz et al. 2006; Martin et al. 2007; Simon & Geha 2007; Geha et al. 2009; Simon et al. 2011).⁵ Furthermore, the ultrafaint dSphs extend a relation under which

⁴M31 hosts several ‘extended’ globular clusters with half-light radii as large as several tens of pc (e.g., Huxor et al. 2005), but no similar population within the Milky Way has yet been discovered.

⁵Some ambiguity regarding the masses of the smallest, faintest dSphs results from the convergence of three relevant quantities—the typical velocity measurement error, the measured velocity dispersions, and the potential contribution to the measured dispersions from binary orbital motions—on the same value, $\sim 3-4$ km s⁻¹ (Simon & Geha 2007; Martin et al. 2007; McConnachie & Côté 2010; Simon et al. 2011; Koposov et al. 2011b). For some faint dSphs the most compelling evidence for large amounts of dark matter comes from stellar-atmospheric chemistry rather than kinematics. The faintest objects classified as dSphs tend to have metallicity dispersions ($\sigma_{[\text{Fe}/\text{H}]} \gtrsim 0.4$ dex, Geha et al. 2009; Norris et al. 2010; Kirby et al. 2011; Willman et al. 2011) that are indicative of prolonged and perhaps multiple episodes of star formation, thereby requiring gravitational potentials sufficiently deep to retain interstellar

less luminous dSphs have larger M/L_V (Mateo et al. 1993; Mateo 1998, Section 5). The discontinuity in dynamical M/L_V between dSphs and globular clusters seems to mark a boundary between objects with dark matter and those without.

3. Stellar Velocity Dispersion as a Proxy for Mass

In rotating spiral galaxies, the circular velocity at radius r relates directly to enclosed mass via $v_{\text{circ}}^2 = GM(r)/r$. Ordered rotation in dSphs is dynamically negligible (see next section); instead, dSphs receive support against gravity primarily from the random motions of their stars. Therefore the estimation of dSph masses is a fundamentally statistical enterprise. The simplest statistic that characterises dSph stellar dynamics is the dispersion of velocities along the line of sight, σ . For a relaxed system of characteristic size R , the virial theorem implies $\sigma^2 \propto GM/R$. In principle, measurements of a dSph’s size and velocity dispersion provide a simple estimate of its mass (Section 4). In practice, one must be aware of effects that can inflate measured values of the velocity dispersion above equilibrium values.

3.1. Rotation

In the simplest case, solid-body rotation about an axis misaligned with the line of sight will induce a gradient, dV/dR , in the line-of-sight velocity distribution. For example, Figure 14 plots mean velocity along the axes for which the observed velocity gradients are maximal in Carina, Fornax, Sculptor and Sextans. Even at the radii of the outermost observed stars, any ordered motion due to rotation is limited to $R_{\text{max}} dV/dR \lesssim 3 \text{ km s}^{-1}$, negligible compared with the observed velocity dispersions of $\sigma \sim 10 \text{ km s}^{-1}$.

For Carina and Fornax the amplitude and orientation of the observed velocity gradients are consistent with a perspective effect induced not by rotation, but rather by these dSphs’ systemic orbital motions transverse to the line of sight (Kaplinghat & Strigari 2008; Walker et al. 2008), as measured from HST astrometry (Piatek et al. 2002, 2003, 2007). The observed signal in Sculptor cannot be attributed to its measured proper motion (Schweitzer et al. 1995; Piatek et al. 2006), and thus Sculptor may have a residual rotational component (Battaglia et al. 2008), albeit one that contributes weakly ($v_{\text{rot}}/\sigma \lesssim 0.5$) to the measured velocity dispersion.

media despite pressures generated by stellar feedback. An adequate discussion of the relationships between dSph kinematics and stellar chemistry is beyond the scope of the present work; Tolstoy et al. (2009) provide an excellent, recent review.

3.2. External Tides

All dSphs considered here orbit within the gravitational potential of the Milky Way and are therefore susceptible to external influence from tidal forces. Tides can affect the structure and kinematics of a given satellite through a variety of mechanisms, including stripping, shocking, ‘stirring’ and various orbital resonances. Depending on the strengths of interactions and timescales of subsequent relaxation, tides might inflate observed velocity dispersions and mass estimates based thereupon.

In the most extreme scenarios, tides have been invoked to explain dSph velocity dispersions without dark matter (e.g., Kuhn & Miller 1989; Kuhn 1993; Kroupa 1997; Fleck & Kuhn 2003; Metz & Kroupa 2007). Such explanations are most plausible for dSphs that are closest to the Milky Way and exhibit elongated stellar structures, e.g., Ursa Major II (Zucker et al. 2006a; Muñoz et al. 2010), Hercules (Belokurov et al. 2007; Coleman et al. 2007; Martin & Jin 2010), and possibly Segue 1 (Niederste-Ostholt et al. 2009). However, generalisation of purely tidal mechanisms to explain the apparent dark matter content of the entire dSph population does not account without contrivance for the wide distribution of dSph distances ($\sim 30 \lesssim D/\text{kpc} \lesssim 250$) or for a monotonic metallicity-luminosity relation (Mateo 1998; Kirby et al. 2008, 2011).

While tidal stripping involves the transfer of mass from the satellite to the parent outside a particular boundary⁶, tidal ‘shocking’ involves impulsive injection of energy into the satellite as it plunges through the disk and/or near the center of the parent system (e.g., Gnedin et al. 1999). While the former process removes mass preferentially from the satellite’s outer regions, the latter process tends to decrease its central density (Read et al. 2006a). Early numerical simulations by Piatek & Pryor (1995) and Oh, Lin & Aarseth (1995) suggest that even strong tidal interactions do not significantly inflate a satellite’s central velocity dispersion, which therefore can remain a reliable indicator of dynamical mass.

Many recent N-body simulations examine specific phenomenology associated with tidal interactions. For example, Read et al. (2006a) use simulations to demonstrate that the projection of tidal streaming motions along most viewing angles tends to cause velocity dispersion profiles to increase at large radius, and then argue that the lack of such upturns in the classical dSphs (with the possible exception of Draco—see Figure 12) limits the severity of current disruption events. Peñarrubia et al. (2008) use simulations to show that repeated tidal encounters cause monotonic declines in equilibrium values (as evaluated at apocenter) of the satellite’s central surface brightness, velocity dispersion and scale radius. Further simulations by Peñarrubia et al. (2009) indicate that when a dark matter halo is present, tides do *not* generate a clear truncation in the surface brightness profile of the bound remnant, as otherwise is prescribed by the self-consistent dynamical model

⁶Equation 4 gives the tidal radius for the idealised case of point-mass potentials. Calculations and simulations by Read et al. (2006b) demonstrate that stars are actually lost from various depths depending on the internal mass distributions of satellite and parent, as well as on the properties of the stellar orbits themselves (e.g., prograde versus retrograde with respect to the orbit of the dSph about the Galaxy).

of King (1966). Rather, as the bound remnant relaxes after a pericentric encounter, tidal debris generates an ‘excess’ of stars at radii where the local crossing time ($R_c/\sigma \sim 10$ Myr at the core radius of a typical dSph) exceeds the time elapsed since the encounter.

Such simulations provide a context for evaluating the tidal origin of breaks and bumps in observed surface brightness profiles of individual dSphs (Section 2.2.3 and Figure 2), and for gauging the severity with which tides influence the observed kinematics. In general, one can expect tides to have stronger and more enduring influence on the outer regions of dSphs, and for the degree of influence on any particular satellite to scale with orbital parameters. A typical dSph with $R_c \sim 100$ pc and $\sigma \sim 10$ km s⁻¹ requires ~ 20 core crossing times to travel a distance of ~ 100 kpc (a typical Galactocentric distance) at speed ~ 250 km s⁻¹; the assumption of dynamic equilibrium should therefore hold reasonably well out to several core radii for the majority of dSphs. In practice one must use all available information about a satellite’s orbit and outer structure to evaluate the likely contribution of tides on a case-by-case basis.

3.3. Binary Stars

Unresolved binary orbital motions might contribute significantly to the observed velocity dispersions of the least massive galaxies. Olszewski et al. (1995) use 112 independent velocity measurements for 42 stars in Draco and Ursa Minor to identify seven stars that exhibit velocity variability. Elimination of these stars from their samples has negligible impact on the measured velocity dispersions of Draco and Ursa Minor. Using the larger KPNO/HYDRA sample of (Armandroff et al. 1995) (373 independent velocity measurements for 185 stars), Olszewski et al. (1996) perform Monte Carlo simulations to estimate that the binary frequency for Draco and Ursa Minor stars with periods of ~ 1 year is ~ 0.2 – 0.3 per decade of period. Even though this fraction is larger than the one found in the solar neighborhood (e.g., Duquennoy & Mayor 1991), further simulations by Olszewski et al. (1996) and Hargreaves et al. (1996a) demonstrate that the scatter introduced by binaries is small compared to the measured dispersions of $\sigma \sim 10$ km s⁻¹, and thus that binaries do not significantly inflate dynamical masses of the ‘classical’ dSphs.

More recently, measurements of velocity dispersions as small as $\sigma \sim 3$ km s⁻¹ for several ultrafaint satellites (Simon & Geha 2007; Martin et al. 2007; Walker et al. 2009a; Adén et al. 2009; Koposov et al. 2011b) have renewed concerns over the possible contribution of binary motions. While simulations by Minor et al. (2010) find that binaries have little effect on dispersions measured for systems with intrinsic velocity dispersions $\sigma \gtrsim 4$ km s⁻¹, complementary simulations by McConnachie & Côté (2010) demonstrate that for systems with intrinsic dispersions near zero (as would be expected for many of the ultrafaints if they contain no dark matter), binaries can inflate measured dispersions to values as high as $\sigma \sim 4$ km s⁻¹.

It is therefore necessary to verify the extreme mass-to-light ratios of the faintest (and coldest) dSphs with repeat spectroscopic measurements that constrain the velocity variability of individual stars. Simon et al. (2011) present second-epoch Keck/DEIMOS velocity measurements for several

of the Segue 1 stars first measured by Geha et al. (2009). They find that one of Segue 1’s six red giants shows significant velocity variability, as do two fainter stars. Including parametric binary orbital distribution functions in a Bayesian analysis of Segue 1’s velocity dispersion, Simon et al. (2011, see also Martinez et al. 2011) estimate a velocity dispersion of $3.7_{-1.1}^{+1.4}$ km s^{−1}, implying a dynamical mass-to-light ratio of $M/L_V \sim 3400[M/L_V]_{\odot}$ and reinforcing their previous conclusion that Segue 1 is the ‘darkest’ galaxy known.

In a separate study, Koposov et al. (2011b) use ~ 15 VLT/FLAMES observations obtained over one month in order to resolve binary motions directly among members of Boötes I. Figure 15 displays independent velocity measurements for two stars as a function of time. While velocities for the star in the left-hand panel are consistent with a constant velocity, velocities for the star in the right-hand panel change systematically by ~ 10 km s^{−1}. After discarding probable binaries, Koposov et al. (2011b) find that most members of Boötes I belong to a cold population with dispersion $\sigma = 2.4_{-0.5}^{+0.9}$ km s^{−1} (Figure 16), significantly smaller than previous single-epoch estimates of $\sigma \sim 6.5$ km s^{−1} (Muñoz et al. 2006; Martin et al. 2007). At present the contribution of binaries to the velocity dispersions measured for the coldest dSphs is poorly understood, and more multi-epoch studies are required.

4. dSph Masses

For a collisionless stellar system in dynamic equilibrium, the gravitational potential, Φ , relates to the phase-space distribution of stellar tracers⁷, $f(\vec{r}, \vec{v}, t)$, via the collisionless Boltzmann Equation (Equation 4-13c of Binney & Tremaine 2008):

$$\frac{\partial f}{\partial t} + \vec{v} \cdot \nabla f - \nabla \Phi \cdot \frac{\partial f}{\partial \vec{v}} = 0. \quad (5)$$

Current instrumentation resolves the internal distributions of neither distance nor proper motions for dSph stars. The structural and kinematic observations described in section 2 provide information only about the projections of phase space distributions along lines of sight, limiting knowledge about f and hence also about Φ . Therefore all efforts to translate existing data sets into constraints on Φ involve simplifying assumptions. Along with dynamic equilibrium, common assumptions include spherical symmetry and particular functional forms for the distribution function and/or the gravitational potential. The most useful analyses identify the least restrictive assumptions that are appropriate for a given data set. Modern structural/kinematic data contain information that is sufficient to place reasonably robust constraints not only on the amount of dSph mass, but in some cases also on its spatial distribution.

⁷The distribution function is defined such that $f(\vec{r}, \vec{v}, t)d^3\vec{r}d^3\vec{v}$ specifies the number of stars inside the volume of phase space $d^3\vec{r}d^3\vec{v}$ centered on $(\vec{r}, \vec{v})$ at time t .

4.1. Amount

4.1.1. ‘Mass Follows Light’ Models

A common method for analysing dSph kinematics employs the following assumptions:

1. dynamic equilibrium;
2. spherical symmetry;
3. isotropy of the velocity distribution, such that $\langle v_r^2 \rangle = \langle v_\theta^2 \rangle = \langle v_\phi^2 \rangle$;
4. a single stellar component;
5. the mass density profile, $\rho(r)$, is proportional to the luminous density profile, $\nu(r)$ (i.e., M/L is constant, or ‘mass follows light’).

Historically, assumption (5) has been adopted when the velocity dispersion profile $\sigma(R)$ is unavailable. Examples include early analyses of classical dSphs (Mateo 1998, and references therein) and initial analyses of ultrafaint dSphs (e.g., Kleyna et al. 2005; Muñoz et al. 2006; Martin et al. 2007; Simon & Geha 2007). Under this assumption, the steeply falling outer surface brightness profiles of dSphs (Section 2.2.1 and Figure 2) motivate the use of dynamical models that allow for truncation by external tides (e.g., Michie 1963; King 1966). Consider, for example, the model of King (1966, see also Chapter 4 of Binney & Tremaine 2008), in which the distribution function depends only on energy:

$$f(\varepsilon) = k(2\pi v_s^2)^{-3/2} (\exp[\varepsilon/v_s^2] - 1). \quad (6)$$

The relative potential, $\Psi \equiv \Phi_0 - \Phi$, is defined such that $\varepsilon \equiv \Psi - \frac{1}{2}v^2 \geq 0$ at radii $r \leq R_K$. Given the assumption that mass follows light, this model is fully specified by dimensionless parameter $\Psi(0)/v_s^2$ (or equivalently, R_K/R_c), the core radius R_c and one of either the central velocity dispersion σ_0 or central mass density ρ_0 , which are all related by $R_c^2 = \frac{9\sigma_0^2}{4\pi G\rho_0}$.

Illingworth (1976) shows that under assumptions (1)-(5) and a distribution function of the form specified by Equation 6, the total mass is given by

$$\frac{M_{\text{tot}}}{M_\odot} = 167\eta \left[\frac{R_c}{\text{pc}} \right] \left[\frac{\sigma^2}{\text{km}^2\text{s}^{-2}} \right], \quad (7)$$

where parameter η is determined by concentration $c \equiv \log_{10}[R_K/R_c]$. Following Mateo (1998), many authors adopt $\eta \approx 8$, which is appropriate for the low concentrations characteristic of classical dSphs but is not well-constrained for the faintest dSphs.

More generally, Richstone & Tremaine (1986) show that for ‘almost any’ spherical, isotropic system with constant mass-to-light ratio and centrally cored luminosity profile, the dynamical mass-to-light ratio is approximately

$$\frac{M}{L} \approx \frac{9\sigma_0^2}{2\pi G\Sigma(0)R_{\text{hb}}}, \quad (8)$$

where the half-brightness radius is defined by $\Sigma(R_{\text{hb}}) = \frac{1}{2}\Sigma(0)$ and is often similar (within $\sim 25\%$) to R_c . Figure 17 plots dynamical mass-to-light ratios calculated from Equation 8 against dSph luminosity. Masses obtained for the Milky Way’s eight classical dSphs are all $M_{\text{tot}} \sim 10^7 M_{\odot}$ (Mateo 1998). For the ultrafaints, masses range from $10^5 \lesssim M_{\text{tot}}/M_{\odot} \lesssim 10^7$ (Martin et al. 2007; Simon & Geha 2007). Dynamical mass-to-light ratios increase monotonically with decreasing luminosity, ranging from $10 \lesssim M/L_V/[M/L_V]_{\odot} \lesssim 1000$.

4.1.2. Does Mass Follow Light?

When available, empirical velocity dispersion profiles provide simple tests of the assumptions listed above. Dashed lines in Figure 12 display best-fitting King (1966, Equation 6) models constructed under assumptions (1)-(5), fit to the surface brightness profiles of Irwin & Hatzidimitriou (1995, Figure 2), and normalised to fit the central velocity dispersions. For all of the Milky Way’s classical dSphs, the central velocity dispersions imply large mass-to-light ratios $M/L_V \gtrsim 10[M/L_V]_{\odot}$, as plotted in Figure 17. However, the mass-follows-light models underpredict the observed velocity dispersions at large radii, which tend to remain approximately constant out to the outermost measured points.

These discrepancies between empirical velocity dispersion profiles and mass-follows-light models in Figure 12 imply that at least one of assumptions (1)-(5) is invalid. In fact *all* are invalid at some level. However, various studies indicate that it is unlikely any one of assumptions (1)-(4) alone can be the problem. For example:

1. Simulations by Read et al. (2006a) suggest that tidal disruption (a violation of the equilibrium assumption) is more likely to generate rising velocity dispersion profiles rather than the flat profiles observed for real dSphs.
2. Axisymmetric models of Fornax considered by Jardel & Gebhardt (2011, see Section 4.2.2) favor dark matter halos that, while violating the assumption of spherical symmetry, extend well beyond the luminous component and therefore also invalidate the mass-follows-light assumption.
3. Evans, An & Walker (2009) derive analytically an expression for the anisotropy profile, $\beta_a(r) \equiv 1 - \langle v_{\theta}^2 \rangle / \langle v_r^2 \rangle$ in terms of surface brightness and velocity dispersion profiles. If mass follows light, then the flat empirical velocity dispersion profiles tend to imply unphysical values $\beta_a > 1$.
4. While recent observations indicate that some dSphs contain at least two distinct stellar subpopulations (Sections 2.2.4 and 4.2.2), scale radii of the individual subpopulations are sufficiently well constrained (e.g., Battaglia et al. 2006; Battaglia et al. 2008) that superpositions of two mass-follows-light models continue to underpredict the observed velocity dispersions at large radii. Indeed Battaglia et al. (2008) find that the flat velocity dispersion profile they measure for Sculptor’s more spatially extended subpopulation continues to imply an even more extended dark matter halo.

Models that allow for sufficiently extended dark matter halos (violating assumption (5) while

retaining assumptions (1)-(4)) can provide good fits to surface brightness and velocity dispersion profiles simultaneously (e.g., Pryor & Kormendy 1990; Wilkinson et al. 2002). On these grounds, the empirical profiles shown in Figures 2 and 12 provide the strongest available evidence that dSphs have dominant dark matter halos that extend beyond luminous regions.

Some scenarios for dSph formation and evolution—particularly the tidal stirring mechanism of Mayer et al. (2001a,b, Section 3.2) and the tidal disruption simulations of Muñoz et al. (2008)—tend to produce configurations in which mass approximately follows light. The results discussed above seem to rule out this configuration. However, Łokas (2009) finds reasonable agreement with mass-follows-light models in Carina, Fornax, Sculptor and Sextans after trimming velocity samples in order to remove member stars classified by an iterative mass estimator (Klimentowski et al. 2007) as unbound. This result rests in part on a circular argument, as the adopted mass estimator (Heisler et al. 1985) is based on the virial theorem, which itself assumes mass follows light. However, the same charge of circularity can be brought against the standard kinematic analysis, in which the inclusion of stars at large radius in the kinematic analysis implicitly assumes they are bound by a sufficiently extended dark matter halo. Thus conclusions regarding the extended structure of dSph dark matter halos are generally sensitive to the assumptions employed when determining which stars to consider or reject in kinematic analyses. More secure is the conclusion that dark matter dominates dSph potentials: even mass-follows-light models require central mass-to-light ratios $M/L_V \gtrsim 10[M/L_V]_\odot$ in order to fit the central velocity dispersions of dSphs (Muñoz et al. 2008; Łokas 2009, and Figure 12).

4.1.3. Jeans Analysis

The methods for mass estimation described in the previous section either employ directly or are derived from specific distribution functions $f(\vec{r}, \vec{v})$ that correspond to physical dynamical models restricted by particular assumptions. Integration of Equation 5 over velocity space provides an alternative starting point in the form of the Jeans equations (see Binney & Tremaine 2008). With spherical symmetry one obtains

$$\frac{1}{\nu} \frac{d}{dr} (\nu \langle v_r^2 \rangle) + 2 \frac{\beta_a \langle v_r^2 \rangle}{r} = - \frac{GM(r)}{r^2}, \quad (9)$$

where $\nu(r)$, $\langle v_r^2 \rangle(r)$, and $\beta_a(r) \equiv 1 - \langle v_\theta^2 \rangle / \langle v_r^2 \rangle$ describe the 3-dimensional density, radial velocity dispersion, and orbital anisotropy, respectively, of the (stellar) tracer component. The mass profile, $M(r)$, includes contributions from any dark matter halo. While there is no requirement that mass follow light, there is also no guarantee that a given solution to Equation 9—even one that fits the data—corresponds to a physical dynamical model (i.e., one for which $f(\vec{r}, \vec{v})$ is non-negative).

Equation 9 has general solution (van der Marel 1994; Mamon & Łokas 2005)

$$\nu \langle v_r^2 \rangle = \frac{1}{f(r)} \int_r^\infty f(s) \nu(s) \frac{GM(s)}{s^2} ds, \quad (10)$$

where $f(r) = 2f(r_1)\exp\int_{r_1}^r \beta_a(s)s^{-1}ds$. Projecting along the line of sight, the mass profile relates to observable profiles, the projected stellar density, $\Sigma(R)$ (Figure 2), and velocity dispersion, $\sigma(R)$ (Figure 12), according to (Binney & Tremaine 2008)

$$\sigma^2(R)\Sigma(R) = 2 \int_R^\infty \left(1 - \beta_a \frac{R^2}{r^2}\right) \frac{\nu \langle v_r^2 \rangle r}{\sqrt{r^2 - R^2}} dr. \quad (11)$$

Equation 11 forms the basis for many methods of mass estimation, including parametric (e.g., Strigari et al. 2006, 2008a; Strigari 2010; Koch et al. 2007b,a; Battaglia et al. 2008; Walker et al. 2007b, 2009b; Martinez et al. 2011) and nonparametric (e.g. Wang et al. 2005) techniques as well as algebraic inversion (e.g., Wilkinson et al. 2004; Gilmore et al. 2007).

All methods based on Equation 11 are limited fundamentally by a degeneracy between the function of interest, $M(r)$, and the anisotropy profile, $\beta_a(r)$, which is poorly constrained by velocity data confined to the line of sight.⁸ Consideration of a common parametric method helps to illustrate this limitation. For example, it is common to assume that the gravitational potential is dominated everywhere by a dark matter halo with mass density profile

$$\rho(r) = \rho_s \left(\frac{r}{r_s}\right)^{-\gamma} \left[1 + \left(\frac{r}{r_s}\right)^\alpha\right]^{\frac{\gamma-\beta}{\alpha}}, \quad (12)$$

i.e., the generalisation by Zhao (1996) of the Hernquist (1990) profile. Equation 12 provides a flexible halo model in the form of a split power-law, with free parameter α controlling the transition from index $-\gamma$ at small radii ($r \ll r_s$) to a value of $-\beta$ at large radii ($r \gg r_s$).

From spherical symmetry, the density profile specifies the mass profile via

$$M(r) = 4\pi \int_0^r s^2 \rho(s) ds \quad (13)$$

and the surface brightness profile specifies the (deprojected) stellar density profile via

$$\nu(r) = -\frac{1}{\pi} \int_r^\infty \frac{d\Sigma}{dR} \frac{dR}{\sqrt{R^2 - r^2}}. \quad (14)$$

Given values for free parameters ρ_s , r_s , α , β , γ and an assumption about the otherwise unconstrained anisotropy profile⁹, Equation 11 specifies a product $\Sigma(R)\sigma^2(R)$ that can then be compared with observations.

⁸Lokas et al. (2005) develop a Jeans analysis that uses higher-order velocity moments (e.g., $\langle v^4 \rangle$) in order to reduce degeneracy between anisotropy (assumed to be constant) and total mass (effectively normalising a cusped mass profile that is assumed to have $\gamma = 1$ in the notation of Equation 12).

⁹Typical assumptions about anisotropy range in simplicity from $\beta_a = 0$ or $\beta_a = \text{constant}$ to $\beta_a(r) = (\beta_\infty - \beta_0)r^2/(r_\beta^2 + r^2) + \beta_0$ (e.g., Strigari 2010), introducing as many as three new free parameters.

Using Sculptor as an example, Figure 18 demonstrates the degeneracy that is inherent in the standard Jeans analysis. Overplotted on Sculptor’s empirical velocity dispersion profile are best-fitting models obtained under specific assumptions either about the inner slope of the mass-density profile ($\gamma = 0$ or $\gamma = 1$), or about the amount of velocity anisotropy ($\beta_a = -0.5$, $\beta_a = 0$ or $\beta_a = +0.3$). Despite corresponding to a wide range of total masses and mass distributions (bottom panels of Figure 18), all of these models can provide equivalent fits to the structural and kinematic data.

While the Jeans analysis provides useful constraints on none of the halo parameters included in Equation 12, it does imply a model-independent constraint on a basic dynamical quantity. All models that fit the velocity dispersion profile give approximately the same value for the enclosed mass near the halfflight radius (middle panel of Figure 18), indicating that this quantity is well determined by the available data. Indeed, formal confidence intervals derived from Markov-Chain Monte Carlo scans of the full parameter space (e.g., Strigari et al. 2007a; Strigari 2010; Walker et al. 2009b; Wolf et al. 2010; Martinez et al. 2011) show a characteristic ‘pinch’ near the halfflight radius (Figure 18).

Equivalent constraints on the enclosed mass at the halfflight radius can be obtained more simply by solving Equation 9 under the assumptions that $\beta_a = 0$ and $\sigma(R) = \text{constant}$. For a Plummer surface brightness profile (Equation 3), one obtains (Walker et al. 2009b)

$$M(R_h) = \frac{5R_h\sigma^2}{2G}. \quad (15)$$

Wolf et al. (2010) show analytically that for various surface brightness and anisotropy profiles, the tightest constraint on the mass profile (provided that the velocity dispersion profile is sufficiently flat) can be approximated by

$$M(r_3) = \frac{3r_3\sigma^2}{G}, \quad (16)$$

where r_3 is the radius at which $d \ln \nu / d \ln r = -3$. For most commonly-adopted surface brightness profiles, this radius is close to the *deprojected* halfflight radius (i.e., the radius of the sphere containing half of the stars), which typically exceeds the projected halfflight radius by a factor of $\sim 4/3$. Insofar as the assumption of flat velocity dispersion profiles (and the usual assumptions of dynamic equilibrium and spherical symmetry) holds, these simple mass estimators can be applied even to the relatively sparse kinematic data available for ultrafaint satellites. Walker et al. (2009b, see erratum for updated values) and Wolf et al. (2010) tabulate masses obtained from Equations 15 and 16, respectively, for ~ 2 dozen Local Group dSphs.

The equivalence of such seemingly crude estimates to constraints from Jeans/MCMC explorations of parameter space follows from a combination of facts: 1) Equation 9 deals only with velocity moments of the phase space distribution function and not with the distribution function itself; 2) confinement of empirical velocity distributions to the line-of-sight component yields little information about β_a ; 3) therefore the flat velocity dispersion profiles of dSphs effectively reduce the available kinematic information to just two numbers, σ and the scale radius that characterises the adopted surface brightness profile. The information extracted from the Jeans analysis naturally amounts to a simple combination of these two numbers.

4.2. Distribution

Some cosmological and particle physics models make specific predictions about how dark matter is distributed within individual halos (Section 6). Insofar as dSphs represent the structures most dominated by dark matter and least affected by the presence of baryons, their internal dynamical properties provide the most straightforward tests of such predictions. Section 4.1.3 demonstrates that so long as dSphs have flat velocity dispersion profiles, the standard Jeans analysis constrains only one number, characterising the amount but not the distribution of dark matter. However, the restrictive assumptions employed in the standard Jeans analysis overlook structure that is present in the data available for many dSphs (Section 2.2.4). Recent analyses that are devised to exploit more fully the available empirical information have been able to place useful constraints not only on the amount, but also on the distribution of dark matter within individual dSphs.

4.2.1. Indirect Constraints

The presence of stellar substructure within dSphs can provide extra leverage not easily exploited in the context of equilibrium dynamical models. For example, it has long been known that Ursa Minor’s stellar component is ‘lumpy’ (Hodge 1964b; Olszewski & Aaronson 1985; Irwin & Hatzidimitriou 1995; Palma et al. 2003, Section 2.2.4). While Ursa Minor has a velocity dispersion of $\sigma \sim 10 \text{ km s}^{-1}$, Kleyna et al. (2003) find that a secondary peak in Ursa Minor’s stellar density field, offset by $\sim 20'$ ($\sim 400 \text{ pc}$) from the nominal center, exhibits a cold dispersion of $\lesssim 1 \text{ km s}^{-1}$. Interpreting this feature as a loosely bound star cluster captured by Ursa Minor, Kleyna et al. (2003) perform N-body simulations to examine how its stability depends on the external gravitational potential (assumed to be dominated by dark matter) of Ursa Minor. Whereas simulated clusters remain intact for a Hubble time when the host potential has a central ‘core’ with constant density ($\gamma = 0$ in the notation of Equation 12) on scales larger than the orbital radius, they disrupt on timescales of $\lesssim 1 \text{ Gyr}$ when the host potential has a centrally divergent, or ‘cusped’ density profile ($\gamma > \frac{1}{2}$). Therefore, if the observed clump indeed corresponds to a star cluster free of its own dark matter component, then its survival provides indirect evidence that the dark matter density of Ursa Minor is constant over the central few-hundred pc.

Substructure in the form of Fornax’s five globular clusters provides another example of indirect evidence for a cored dSph potential. Four of these clusters are projected near (within a factor of ~ 2) Fornax’s half-light radius ($R_h \sim 670 \text{ pc}$; Irwin & Hatzidimitriou 1995). Hernandez & Gilmore (1998) show analytically that the rate at which the orbits of such clusters decay due to dynamical friction depends on the underlying dSph potential. Subsequent numerical simulations by Sánchez-Salcedo et al. (2006) and Goerdt et al. (2006) demonstrate that in a cusped potential, dynamical friction would require only a few Gyr to bring the clusters from their present positions (assuming the projected distances from Fornax’s center are not much smaller than the true distances) all the way to Fornax’s center. On the other hand, in a cored potential dynamical friction would bring the clusters only as close as the core radius, where the harmonic potential inhibits further decay. Thus

these considerations provide indirect evidence for a core of constant density over the central few-hundred pc in Fornax. Further simulations by Goerdt et al. (2010) and Cole et al. (2011) suggest that the transfer of angular momentum from a sinking cluster to the central dark matter is capable of *transforming* an originally cusped into a cored potential, a possibility that might be relevant for the interpretation of evidence for cored dark matter halos in some dSphs (Section 6.1).

4.2.2. Constraints from Models

Several groups have recently developed dynamical and/or kinematic models that exploit structure that is present in dSph data but is not considered in the Jeans analyses discussed in Section 4.1.3. For example, the discoveries of two chemo-dynamically independent stellar sub-populations in Sculptor (Tolstoy et al. 2004, Section 2.2.4), Fornax (Battaglia et al. 2006) and Sextans (Battaglia et al. 2011) enable analyses of two tracer components in the same potential. After imposing a metallicity cutoff to separate Sculptor’s two sub-populations, Battaglia et al. (2008) find that cored rather than cusped potentials provide better simultaneous fits in a Jeans analysis (Section 4.1.3) of the two sets of surface brightness and velocity dispersion profiles. Using the same empirical profiles for Sculptor, Amorisco & Evans (2012) confirm this result by modelling both sub-populations with anisotropic King-Michie (King 1962; Michie 1963; King 1966) distribution functions. These dynamical models again favor cored ($\gamma = 0$) rather than cusped ($\gamma = 1$) potentials, with a likelihood ratio sufficient to reject the hypothesis of cusped potentials with confidence $\gtrsim 99\%$.

Jardel & Gebhardt (2011) take a different approach, constructing axisymmetric three-integral Schwarzschild (1979) models for both cored and cusped potentials that also allow for a central black hole. For a given potential, libraries of stellar orbits are calculated and each orbit receives a weight based on fits to the observed distribution of velocities within discretely binned radii. Notice that while the Jeans analysis is sensitive only to the variance of the velocity distribution in a given bin, the Schwarzschild method is sensitive to the *shape* of the distribution. Jardel & Gebhardt (2011) find that their models constructed from cored potentials fit Fornax’s velocity data significantly better than those constructed from cusped potentials. Within the context of their adopted models, they also place an upper limit of $\lesssim 3.2 \times 10^4 M_\odot$ on the mass of any central black hole. Breddels et al. (2012) independently develop Schwarzschild models for Sculptor, concluding that the available data rule out steep cusps ($\gamma \gtrsim 1.5$) but are consistent with slopes in the range $0 \lesssim \gamma \lesssim 1$.¹⁰

¹⁰Chanamé et al. (2008) have formulated a Schwarzschild method that operates on discrete velocity measurements, avoiding the binning procedure altogether. Efforts to apply this and other discrete Schwarzschild methods to dSph data are underway. As these and other methods for analysing the shapes of dSph velocity distributions continue to develop, it will be beneficial and perhaps necessary to allow for contributions from multiple stellar populations. Failure to consider distinct populations can generate spurious conclusions regarding orbital structure. To see why this is so, consider that the superposition of two Gaussian distributions need not be Gaussian.

4.2.3. Direct Measurement

Walker & Peñarrubia (2011) introduce a method for measuring the slopes of dSph mass profiles directly from spectroscopic data and without adopting a dark matter halo model. For a given dSph, Walker & Peñarrubia (2011) use measurements of stellar positions, velocities and spectral indices to estimate half-flight radii and velocity dispersions for as many as two chemodynamically independent stellar sub-populations. Detections of two distinct sub-populations with different sizes provide mass estimates $M(R_h) \propto R_h \sigma^2$ (e.g., Equation 15) at two different radii in the same mass profile, immediately specifying a slope. For Fornax and Sculptor, this method yields slopes of $\Gamma \equiv \Delta \log M / \Delta \log r = 2.61^{+0.43}_{-0.37}$ and $\Gamma = 2.95^{+0.51}_{-0.39}$, respectively, on scales defined by values $\sim 0.2 \lesssim R_h/\text{kpc} \lesssim 1$ estimated for the half-flight radii. These slopes are consistent with cored ($\gamma = 0$) potentials, for which $\Gamma \leq 3$ at all radii, but incompatible with cusped ($\gamma \gtrsim 1$) potentials, for which $\Gamma \leq 2$ (Figure 19).

5. A Common dSph Mass?

Mateo et al. (1993) noticed that dSph dynamical mass-to-light ratios increase monotonically with decreasing luminosity (left panel of Figure 17). Based on mass-follows-light analyses (Section 4.1.1), the Milky Way’s eight classical dSphs trace a relationship $\log_{10}(M/L_V/[M/L_V]_\odot) \sim 2.5 + 10^7 L_V/L_{V,\odot}$ (Mateo 1998). This relation implies that if their *stellar* mass-to-light ratios are $M/L_V \sim 2.5[M/L_V]_\odot$, then each dSph is embedded in a dark matter halo of mass $\sim 10^7 M_\odot$. Allowing for extended dark matter halos, Mateo et al. (1993) and Mateo (1998) interpret this value as the minimum mass that is associated empirically with dark matter.

Kinematic studies of the newfound ultrafaint satellites alter this picture slightly. The ultrafaint dSphs extend the luminosity floor from $M_V \sim -9$ (e.g., Draco, Ursa Minor) to $M_V \sim -2$ (e.g., Segue 1), nearly three orders of magnitude in luminosity. Applying mass-follows-light models to their velocity data for the least luminous dSphs, Martin et al. (2007) and Simon & Geha (2007) estimate dynamical masses as small as $\sim 10^5 M_\odot$. While these masses imply extreme mass-to-light ratios $M/L_V \gtrsim 100[M/L_V]_\odot$ that extend the monotonic increase in M/L_V with decreasing luminosity, they suggest that this relationship becomes flatter toward the smallest luminosities (right panel of Figure 17).

Strigari et al. (2008a) extend to ultrafaint satellites the notion of a common dSph mass by considering the amount of mass enclosed within a fixed radius of 300 pc (implicitly assuming that all dSphs occupy dark matter halos at least this large). Using a Jeans analysis similar to that described in Section 4.1.3, Strigari et al. (2008a) estimate $M_{300} \equiv M(r \leq 300\text{pc}) \sim 10^7 M_\odot$ for dSphs spanning five orders of magnitude in luminosity (Figure 20, left panel). Walker et al. (2009b) take a different approach, using the model-independent estimates of $M(R_h)$ provided by Equation 15 to evaluate the hypothesis that all dSphs are embedded in identical dark matter halos characterised by a ‘universal’ mass profile (Figure 20, right panel). While the scatter of $M(R_h)$ values about a

single power law, $M(r) \propto r^x$, is larger (by a factor of ~ 2) than the scatter expected to arise from observational errors, it is similar to the scatter about a common value of M_{300} .

While it has long been known that dSphs do not fit naturally onto scaling relations defined by larger elliptical galaxies (e.g., Kormendy 1985), the roughly exponential decline of dSph surface brightness profiles (Section 2.2.1) hints at a structural relationship to spirals (Faber & Lin 1983; Lin & Faber 1983), perhaps via an evolutionary mechanism such as tidal stirring (Sections 2.2.1, Mayer et al. 2001a,b). Converting estimates of $M(R_h)$ to circular velocities $v_{\text{circ}}^2 = GM(R_h)/R_h$, Walker et al. (2010) find that the Milky Way’s dSph satellites lie on an extrapolation of the mean rotation curve estimated for dark matter in spiral galaxies (Figure 21, left panel), $\log_{10}[V_{\text{circ}}/(\text{kms}^{-1})] = 1.5 + 0.5 \log_{10}[r/\text{kpc}]$ (McGaugh et al. 2007). Donato et al. (2009) and Salucci et al. (2011) find similar results: assuming cored dark matter halos of the form $\rho(r) = \rho_0 r_0^3 (r + r_0)^{-1} (r^2 + r_0^2)^{-1}$ (Burkert 1995), fits to dSph velocity dispersion profiles extend a simple scaling relationship that is common to spiral galaxies (Kormendy & Freeman 2004) and is characterised by $\log_{10}[\rho_0/(M_{\odot} \text{pc}^{-3}) r_0/\text{pc}] \sim 2$, independently of luminosity (Figure 21, right panel).

These scaling relationships have provoked a variety of disparate interpretations. For example, Boyarsky et al. (2010a) show analytically that ‘secondary infall’ of dark matter onto isolated halos would cause surface density to vary slowly with halo mass, explaining the apparent constancy of $\rho_0 r_0$ over the range spanned by spirals. They argue that the apparent extension to dSphs agrees with results from cosmological N-body simulations (e.g., Springel et al. 2008), which produce satellite halos with approximately the same surface density. On the other hand, McGaugh & Wolf (2010) show that dSphs deviate from another spiral scaling relation—the baryonic Tully-Fisher relation (‘BTF’, McGaugh et al. 2000)—systematically according to the amount by which their half-light radii exceed their tidal radii, provided that the latter radius is estimated using Milgrom’s (1983) Modified Newtonian Dynamics (a framework that naturally implies the BTF relation).

In any case, scatter among the Milky Way’s dSphs increased when Adén et al. (2009) and Koposov et al. (2011b) measured smaller velocity dispersions for Hercules and Boötes I, respectively, than had previously been estimated (Section 2.3). Furthermore, early kinematic results for the dSph satellites of M31 suggest systematically smaller masses (at a given half-light radius) than estimated for the Milky Way dSphs (Kalirai et al. 2010; Collins et al. 2010, 2011). However, more recent, larger data sets suggest that the M31 dSphs are more similar to the MW dSphs than previously suggested (Tollerud et al. 2011). Pending more detailed spectroscopic surveys, particularly of the least luminous and most distant dSphs, the interpretation of scaling relationships that connect galaxies across such wide ranges of luminosity and morphological type should proceed with caution.

6. Implications for Cosmology and Particle Physics

Observations indicate that the Milky Way’s known dSph satellites have masses $10^5 \lesssim M(R_h)/M_{\odot} \lesssim 10^7$ and that dark matter dominates their internal kinematics at all radii, $M/L_V \gtrsim 10[M/L_V]_{\odot}$ (Sec-

tion 4.1). Current observations also provide direct and/or indirect constraints on the internal distributions of dark matter in three dSphs: Fornax, Sculptor and Ursa Minor (Section 4.2). For all three, the available evidence indicates central ‘cores’ of constant density on scales of a few hundred pc.¹¹ Taken at face value, these basic results have implications for broader areas of physics.

6.1. Cosmology

Observations of structure on large scales (e.g., as inferred from redshift surveys and anisotropy of the cosmic microwave background radiation) seem to require a significant contribution to the mass budget from non-baryonic dark matter, $\Omega_{\text{DM}} \sim 0.22$ (e.g, Bennett et al. 2003; Spergel et al. 2003). The ‘cold dark matter’ (CDM) cosmological paradigm is built on the hypothesis that the dark matter consists of fundamental particles that act like a collisionless gas after decoupling from radiation at non-relativistic speeds shortly after the Big Bang. Small cross sections and low thermal velocities allow CDM structure to form and survive at high densities in small volumes, thereby enabling the growth of structure on small scales in the early universe.

Calculations of the matter power spectrum associated with popular ‘weakly interacting massive particle’ (WIMP) candidates for the dark matter (e.g., neutralinos with mass $m_\chi \gtrsim 10$ GeV) indicate $P(k) \propto k^{-3}$ at small scales until collisional damping and free streaming finally cause an exponential decline on sub-parsec (co-moving) scales (Green et al. 2004; Diemand et al. 2005a). The corresponding halo mass function would be approximately $dN(M)/dM \propto M^{-\alpha}$ with $\alpha \sim 1.9$, and a galaxy like the Milky Way would host roughly $\sim 10^{15}$ satellites in the form of individual, self-bound dark matter ‘subhalos’, ‘sub-subhalos’, ..., and ‘microhalos’ with masses $\gtrsim 10^{-6}M_\odot$ (Hofmann et al. 2001; Diemand et al. 2005a; Springel et al. 2008).

Observational requirements derived from the current census of Milky Way satellites seem rather modest in this context. A viable dark matter particle needs to accommodate the formation and survival of only a few tens (or hundreds when correcting for incompleteness of sky surveys, Koposov et al. 2008; Tollerud et al. 2008) of dark matter halos with masses $M \gtrsim 10^5 M_\odot$ (Section 4) around the Milky Way. These constraints allow for significantly less massive, ‘warmer’ particle candidates (e.g., the sterile neutrino, Dodelson & Widrow 1994; see recent reviews and discussion by, e.g., Abazajian & Koushiappas 2006; Boyanovsky 2008; Boyarsky et al. 2009b; Kusenko 2009) whose longer free-streaming lengths might naturally truncate the matter power spectrum at scales more similar to those that characterise the smallest galaxies (Gilmore et al. 2007; Bode et al. 2001;

¹¹In a recent preprint, Wolf & Bullock (2012) argue that the situation is more ambiguous, and specifically that the Sculptor data of Walker, Mateo & Olszewski (2009) favor a dark matter halo that is centrally cusped ($\gamma = 1$) rather than cored ($\gamma = 0$). Their Figure 1 demonstrates that this conclusion—and more generally the ability of their Jeans analysis to yield an apparent constraint on γ —depends critically on their assumption that the data sample a single stellar population with isotropic ($\beta_a = 0$ in the notation of Equation 11) velocity distribution. This assumption is incompatible with the multi-component structure that is present in the spectroscopic data (Tolstoy et al. 2004; Battaglia et al. 2006; Walker & Peñarrubia 2011, see Sections 2.2.4 and 4.2).

Macciò & Fontanot 2010; Polisensky & Ricotti 2011; Lovell et al. 2012).

Thus dark matter particle candidates and associated cosmologies can be classified in practical terms according to whether the particles’ free streaming plays a significant role in galaxy formation (e.g., Bøhm et al. 2001). For sufficiently massive and ‘cold’ particles it does not, and other physical processes must be invoked to explain the suppression and/or truncation of galaxy formation in low-mass halos (e.g., Klypin et al. 1999; Koposov et al. 2009; Li et al. 2010; Macciò et al. 2010; Kravtsov 2010; Font et al. 2011). The negligible thermal velocities invoked for ‘standard’ CDM particles also imply that N-body simulations can track the growth of structure accurately with relatively few particles, making CDM cosmological simulations the simplest, fastest and most widely practiced kind.

Cosmological simulations demonstrate that if gravitational interactions between standard CDM particles dominate the formation and evolution of galactic structure, then galaxies ought to be embedded in dark matter halos that have central cusps characterised by $\lim_{r \rightarrow 0} \rho(r) \propto r^{-\gamma}$, with $\gamma \gtrsim 1$ (e.g., Dubinski & Carlberg 1991; Navarro, Frenk & White 1996, 1997; Moore et al. 1998; Klypin et al. 2001; Diemand et al. 2005b; Springel et al. 2008). Observations indicate that most individual galaxies with suitable measurements are not embedded in such halos. Instead, rotation curves of spiral and low surface brightness galaxies tend to favor dark matter halos with resolved ‘cores’ ($\gamma \sim 0$) of constant density (e.g., Moore 1994; Flores & Primack 1994; de Blok & McGaugh 1997; Salucci & Burkert 2000; McGaugh et al. 2001; Simon et al. 2005; Kuzio de Naray et al. 2006, 2008, de Blok 2010, and references therein). These results imply that (standard) gravitational interactions between CDM particles do not always dominate the formation and evolution of galactic structure.

Indeed galaxies contain baryons prone to interact via forces other than gravity. Many hydrodynamical simulations demonstrate that various poorly-understood baryon-physical mechanisms might influence the structure of galactic CDM halos (e.g., Blumenthal et al. 1986; Navarro et al. 1996; El-Zant et al. 2001; Gnedin et al. 2004; Tonini et al. 2006; Romano-Díaz et al. 2009; Del Popolo 2010; Governato et al. 2010; Pontzen & Governato 2011; Governato et al. 2012). Insofar as their baryons are dynamically negligible, dSphs and low surface brightness galaxies enable the most direct comparisons to structures formed in CDM-only simulations. In this context the available evidence against cusped dark matter halos in Fornax, Sculptor and Ursa Minor (Section 4.2) becomes particularly relevant: the viability of standard CDM now requires that baryon-driven mechanisms can have *reduced* the central dark matter densities in these galaxies to $\rho_0 \gtrsim 5 \times 10^7 M_\odot \text{kpc}^{-3}$ while leaving behind stellar populations with low luminosities $10^5 \lesssim L_V / L_{V,\odot} \lesssim 10^7$ and central surface brightnesses $23 \lesssim \mu_0 / (\text{mag/arcsec}^2) \lesssim 25$.¹²

Recent work identifies several mechanisms that might accomplish this feat on dSph scales

¹²Boylan-Kolchin et al. (2011) identify a similar (perhaps the same) structural problem, noting that the most massive ‘subhalos’ produced in the *Aquarius* CDM simulation (Springel et al. 2008) have central densities larger than those estimated for any of the known dSphs.

by invoking either the dynamical coupling of the dark matter to energetic baryonic outflows (e.g., Read & Gilmore 2005; Mashchenko et al. 2006, 2008; de Souza et al. 2011) or the transfer of energy/angular momentum to dark matter from massive infalling objects (e.g., Sánchez-Salcedo et al. 2006; Goerdt et al. 2006, 2010; Cole et al. 2011). Hydrodynamical simulations by Sawala et al. (2010) and Parry et al. (2011) indicate that the former category of solutions has difficulty reproducing other dSph observables—specifically, star formation histories as well as luminosity functions and metallicity distributions. The latter category of solutions is difficult to evaluate observationally, as the evidence can literally be destroyed (e.g., by tidal disruption); furthermore it seems unlikely that such infall mechanisms generate cores of sufficient size.¹³ Alternatively, cosmological simulations that consider ‘warmer’ particle candidates demonstrate that the associated suppression of small-scale power can naturally (i.e., without invoking baryon physics) produce halos with large cores; however, such scenarios seem to require fine tuning of the relative contributions from various production mechanisms in order to reproduce simultaneously the number of observed MW dSphs (Polisensky & Ricotti 2011; Macciò et al. 2012a,b).

In any case, the emerging challenge for the standard CDM paradigm is not that empirical evidence against cusped dark matter halos necessarily rules out the hypothesis that CDM particles constitute the dark matter. The poorly understood complexities of baryon physics—along with the freedom to invoke other processes, e.g., self-scattering of CDM particles (Spergel & Steinhardt 2000; Loeb & Weiner 2011; Vogelsberger et al. 2012)—leave sufficient flexibility for CDM to be rendered consistent with virtually any realistic observation of galactic structure. In fact that is the problem. CDM escapes falsification of perhaps its most famous prediction only by withdrawing the prediction. While this circumstance does not imply that CDM is incorrect, it does mean that CDM currently fails to make accurate predictions regarding the stellar dynamics of galaxies, a primary piece of evidence for dark matter in the first place. In this context a decisive outcome favorable to standard CDM seems to require the detection of either 1) gravitational interactions involving dark matter halos on sub-galactic scales (e.g., via microlensing or perturbations of loosely bound luminous structure) or 2) nongravitational interactions involving cold dark matter particles.

6.2. Particle Physics

It has long been recognised that the small sizes and large mass densities of dSphs place strong constraints on the particle nature of dark matter. For example, Liouville’s theorem requires that the phase space densities of light, neutral lepton species do not increase after decoupling from radiation in the early Universe. Tremaine & Gunn (1979) point out that this constraint, combined with the necessity that $\Omega_\nu < \Omega_{\text{matter}}$, places a conservative upper limit on the neutrino mass that is

¹³For example, Goerdt et al. (2010) conclude that a sinking object of mass M_s induces core formation inside a radius where the enclosed halo mass is $M(r_{\text{core}}) \sim M_s$. In this scenario the sinking of Fornax’s five surviving globular clusters ($M_s \sim 10^5 M_\odot$) cannot have formed the core inferred from estimates $M(\sim 550\text{pc}) \sim 5 \times 10^7 M_\odot$ and $M(\sim 900\text{pc}) \sim 2 \times 10^8 M_\odot$ (Walker & Peñarrubia 2011).

summarily violated by lower limits from phase space densities inferred for galaxy halos. Therefore neutrinos are not the dark matter in galaxies. This exclusion is most evident on small scales, where small volumes demand heavy particles in order to satisfy phase-space requirements.

For example, using Aaronson’s (1983) initial measurement of Draco’s velocity dispersion, Lin & Faber (1983) derive a lower limit of $m_\nu \gtrsim 500$ eV. Lake (1989) points out that this constraint is sensitive to the dubious assumption that mass follows light (Section 4.1.1). Gerhard & Spergel (1992) strengthen the argument by turning it around, noting that for more viable neutrino masses of $m_\nu \sim 30$ eV, the core radii of dSph halos would need to be unrealistically large ($\gtrsim 10$ kpc) to accommodate model-independent lower limits of $\rho_0 \gtrsim 0.05 M_\odot \text{pc}^{-3}$ (Pryor & Kormendy 1990) on their central densities. Generalising the phase-space argument of Tremaine & Gunn (1979) to relativistically decoupled warm dark matter candidates, Dalcanton & Hogan (2001) show that of all galaxies, dSphs provide the most stringent limits, $m_\chi \gtrsim 700$ eV and $m_\chi \gtrsim 300$ eV for thermal and degenerate fermions, respectively. Most recently and more specifically, Boyarsky et al. (2009a) use phase-space arguments to conclude that $m_\chi \gtrsim 1.7$ keV if the dark matter consists of sterile neutrinos produced via non-resonant mixing with active neutrinos.

Any positive identification of a dark matter particle will require the detection of its non-gravitational interactions. Experiments at the Large Hadron Collider might find evidence for such interactions, as might the various experiments designed to detect directly the scattering of dark matter particles in Earth’s orbital path. Alternatively, high-energy photons might be released if dark matter self-annihilates (Gunn et al. 1978; Stecker 1978) or decays (Pal & Wolfenstein 1982; Boyarsky et al. 2006; Kusenko 2006), providing an opportunity for indirect detection.

Their large mass-to-light ratios, low astrophysical backgrounds and close proximities make the Milky Way’s dSph satellites popular targets in the search for annihilation and/or decay products (e.g., Evans et al. 2004; Strigari et al. 2008b; Kuhlen 2010). For annihilation, the differential γ -ray flux (units $\text{cm}^{-2} \text{s}^{-1} \text{sr}^{-1} \text{GeV}^{-1}$) received on Earth in solid angle $\Delta\Omega$ is given by

$$\frac{d\Phi_\gamma}{dE_\gamma} = \frac{1}{4\pi} \frac{\langle\sigma v\rangle}{2m_\chi^2} \cdot \frac{dN_\gamma}{dE_\gamma} \times J(\Delta\Omega), \quad (17)$$

where m_χ is the particle mass, $\langle\sigma v\rangle$ is the (velocity-averaged) cross section, dN_γ/dE_γ is the energy spectrum of products and

$$J(\Delta\Omega) = \int_{\Delta\Omega} \int \rho^2(l, \Omega) dl d\Omega. \quad (18)$$

This ‘ J -factor’ represents the astrophysical contribution to the signal and is specified by the integral of the squared dark matter density, $\rho^2(l, \Omega)$, over line of sight l and solid angle Ω . The equation for the flux due to decay events is similar, except that the integral is taken over the dark matter density raised only to the first power. Published constraints on J come directly from constraints on $\rho(r)$ obtained in parametric Jeans analyses of the sort described in Section 4.1.3 and demonstrated in Figure 18 (e.g., Strigari et al. 2007b; Martinez et al. 2009; Charbonnier et al. 2011).

At present, dSph surveys conducted with atmospheric Cherenkov telescopes (e.g., Pieri et al. 2009; Essig et al. 2009; H. E. S. S. Collaboration et al. 2011; the VERITAS collaboration: Vivier et

al. 2011; Aleksić et al. 2011), x-ray (e.g., Boyarsky et al. 2007; Loewenstein et al. 2009; Riemsdijk & Hansen 2009; Loewenstein & Kusenko 2010; Boyarsky et al. 2010b; Loewenstein & Kusenko 2012) and gamma-ray telescopes (e.g., Abdo et al. 2010; Scott et al. 2010; Ackermann et al. 2011) yield no unambiguous detections.¹⁴ From Equation 17, upper limits on photon flux translate into upper limits on the cross section $\langle\sigma v\rangle$ for a given particle mass and annihilation channel. For example, Figure 22 plots 95% upper limits on $\langle\sigma v\rangle$ derived from Fermi-LAT observations of Milky Way dSphs, based on two years of data from the planned five-year mission (Geringer-Sameth & Koushiappas 2011; Ackermann et al. 2011). Dotted lines at $\langle\sigma v\rangle \sim 3 \times 10^{-26} \text{ cm}^3\text{s}^{-1}$ mark the ‘generic’ cross section expected for WIMPs with mass $m_\chi \sim 0.1 - 1 \text{ TeV}$ (e.g., Jungman et al. 1996; Feng 2010). WIMPs having this combination of mass and cross section would have decoupled from radiation with relic abundance $\Omega_{\text{WIMP}} \sim 0.2$, the value cosmology requires of the dark matter (a coincidence sometimes referred to as the ‘WIMP miracle’). For particle masses below $m_\chi \lesssim 100 \text{ GeV}$, the combination of kinematic and high-energy data available for dSphs is now encroaching upon the cross section most readily associated with WIMPs.¹⁵ Over the next decade, searches for dark matter and/or its byproducts will intensify with large-scale efforts at existing facilities and with new instrumentation that will provide unprecedented sensitivity (e.g., CTA Consortium 2010).

The status of dark matter as a particle will depend critically on the outcomes of direct and indirect dark matter detection experiments that are either ongoing or planned for the near future. Also at stake is the motivation and context for studying dark matter phenomenology in dSphs. An unambiguous, positive detection of dark matter byproducts emitted from dSphs would establish the existence of a new particle and would provide a unique means for measuring its mass and cross section; via Equation 17, constraints on such parameters would be only as good as dynamical constraints on the dark matter density profile. In case of detections in other objects, e.g., the Galactic center (see Hooper & Linden 2011) or galaxy clusters (see Han et al. 2012), high-energy and dynamical constraints from dSphs would provide important consistency checks in the regime of minimal astrophysical background. In the case of direct detection and characterisation of a new

¹⁴Loewenstein & Kusenko (2010) interpret a *Chandra* detection of monochromatic ($\sim 2.5 \text{ keV}$) emission from the direction of the Willman 1 satellite as a possible signal of sterile neutrino decay. However, Boyarsky et al. (2010b) argue that non-detections of this feature in the Galactic halo, M31 and several other dSphs rule out a dark matter origin. Indeed, Loewenstein & Kusenko (2012) report no detection of the $\sim 2.5 \text{ keV}$ feature in follow-up XMM-Newton observations of Willman 1; corresponding limits on the mass/mixing angle of sterile neutrinos depend on how reliably the ‘irregular’ stellar kinematics of Willman 1 (Willman et al. 2011, Section 2.2.4) trace its mass.

¹⁵Charbonnier et al. (2011) use published kinematic data to estimate less stringent limits of $\langle\sigma v\rangle \lesssim 10^{-25} \text{ cm}^3\text{s}^{-1}$ (at $m_\chi \sim 10 \text{ GeV}$, cf. Figure 22) for individual dSphs. Possible reasons for this discrepancy include different assumptions about the dark matter halo profile (Geringer-Sameth & Koushiappas 2011 and Ackermann et al. 2011 adopt J values previously estimated under the assumption that dSph dark matter halos follow NFW ($\gamma = 1$ in the notation of Equation 12) profiles; Charbonnier et al. 2011 estimate J values by marginalising over uncertain halo shape parameters), different assumptions about the energy spectrum (Geringer-Sameth & Koushiappas 2011 and Ackermann et al. 2011 explicitly consider annihilation via $b\bar{b}$ and $\tau^+\tau^-$ mechanisms; Charbonnier et al. 2011 consider a conservative spectrum averaged over a variety of plausible annihilation channels) and/or different assumptions about detector sensitivity.

particle in the laboratory, dSph phenomenology would help to establish or rule out association with cosmological dark matter. In case of failure to detect non-gravitational interactions involving dark matter particles, consideration of the extreme phenomenology exhibited by dSphs would help to inform alternative explanations for dark matter.

7. Some Considerations for Future Work

Topics and/or questions for future investigations include the following:

- The least luminous galaxies are often disproportionately interesting. What sorts of bound stellar/gaseous objects will the next generation of sky surveys detect?
- This field will continue to develop in proportion to 1) the rate at which data sets grow in size and quality and 2) the efficiency with which analytical tools can extract the information contained therein. Promising strategies for analysis include the formulation of statistical likelihood functions that depend on discrete measurements (e.g., of individual stellar positions and velocities) rather than on binned profiles, and exploitation of multi-component structure/substructure that is present in the data.
- All dSphs clearly deviate from the simple models invoked to characterise their observed properties. In order to understand dSphs as galaxies, one must consider not only the structural and kinematic data emphasised above, but also chemical abundances, star formation histories (i.e., *stellar* masses), internal substructure and external environment.
- The outer stellar structures of dSphs carry valuable information about the gravitational competition between the Milky Way and its satellites. Combined with deep photometric surveys that map the Galactic stellar halo, wide-field spectroscopic surveys that reach large galactocentric distances in dSphs will reveal details of the transition from satellite to host potential.
- The standard CDM hypothesis seems to require baryon-physical processes to have formed large constant-density cores in galactic dark matter halos. Do the internal mass distributions of galaxies correlate with other observables directly related to baryon physics (e.g., luminosity, metallicity, star formation history)? Constraints on core sizes for the least luminous dSphs would be extremely valuable.
- Can observations and/or experiments provide clear evidence for non-gravitational interactions involving a dark matter particle? Can observations provide evidence for gravitational interactions involving dark matter halos on subgalactic scales?
- Are there cosmological and/or particle physics models for dark matter from which can be extracted accurate predictions regarding the stellar dynamics of the most dark-matter dominated galaxies?

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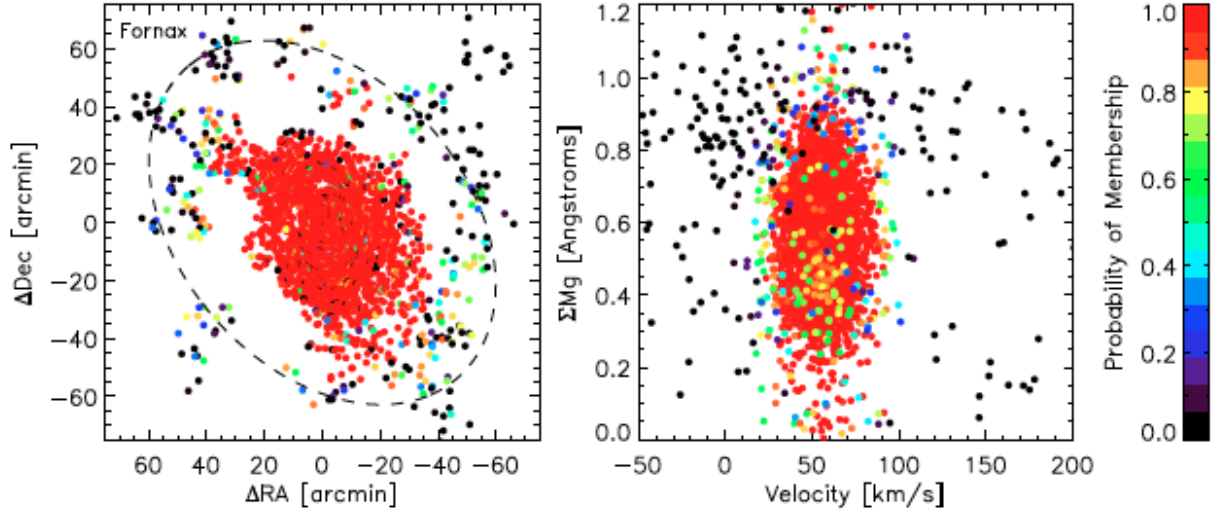


Fig. 11.— Magellan/MMFS spectroscopic data for Fornax (Walker, Mateo & Olszewski 2009, updated to include the full sample of ~ 3200 members). *Left*: Sky positions of individual stars. *Right*: velocities and spectral indices (pseudo-equivalent widths of the Mg-triplet absorption feature). Color indicates membership probability, as estimated from position, velocity and spectral index distributions. The ellipse indicates the limiting radius, R_K (Equation 1).

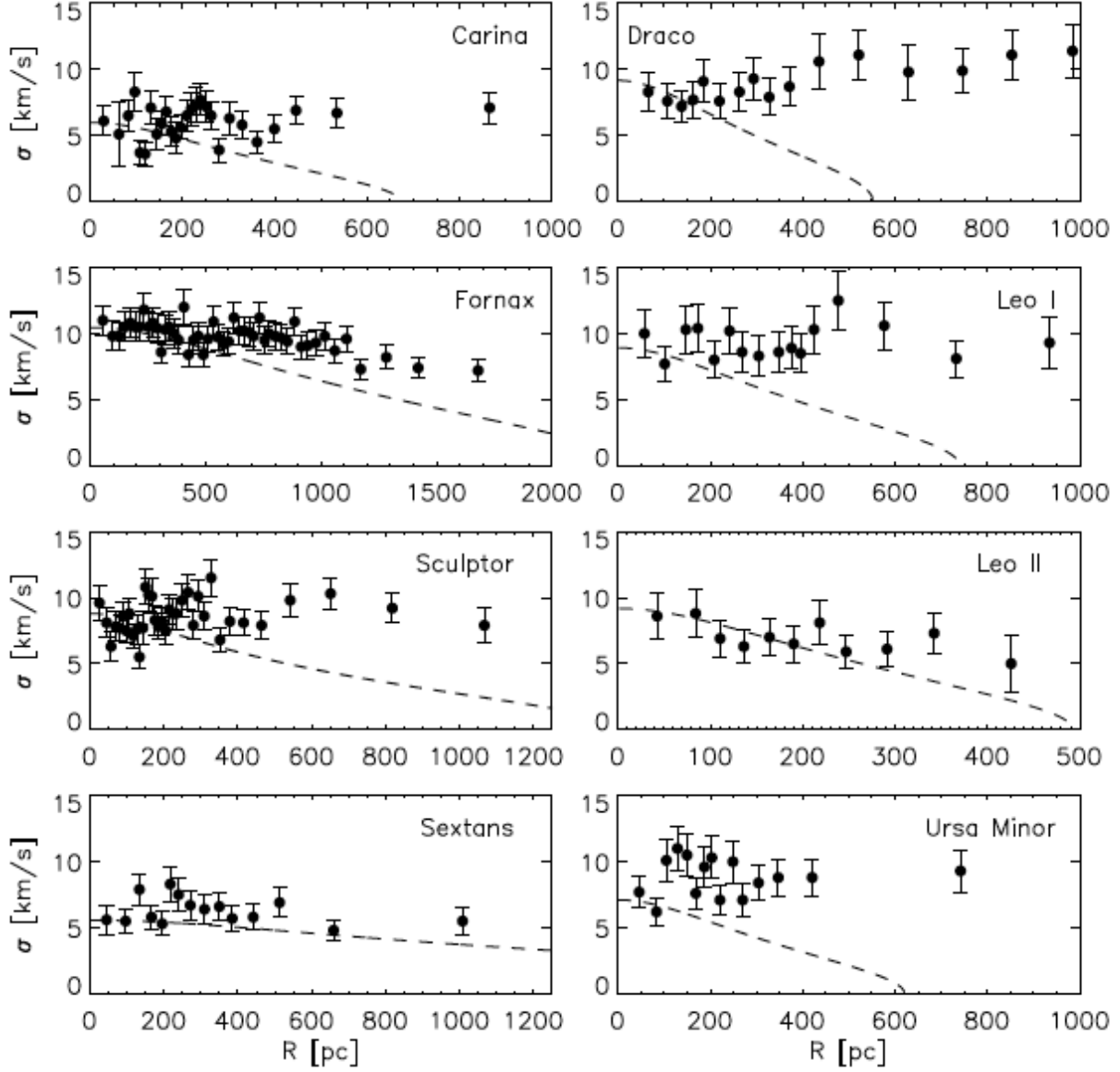


Fig. 12.— Velocity dispersion profiles observed for the Milky Way’s eight ‘classical’ dSphs (Walker et al. 2007a; Mateo et al. 2008; Walker et al. 2009b). See also Kleyna et al. (2002, 2004); Wilkinson et al. (2004); Muñoz et al. (2005, 2006); Sohn et al. (2007); Koch et al. (2007b,a); Battaglia et al. (2008, 2011). Overplotted are mass-follows-light King (1966) models (Section 4.1.1) normalised to reproduce the observed central dispersions. Failure of these models to reproduce the large velocity dispersions at large radius provides the strongest available evidence that dSphs have dominant and extended dark matter halos.

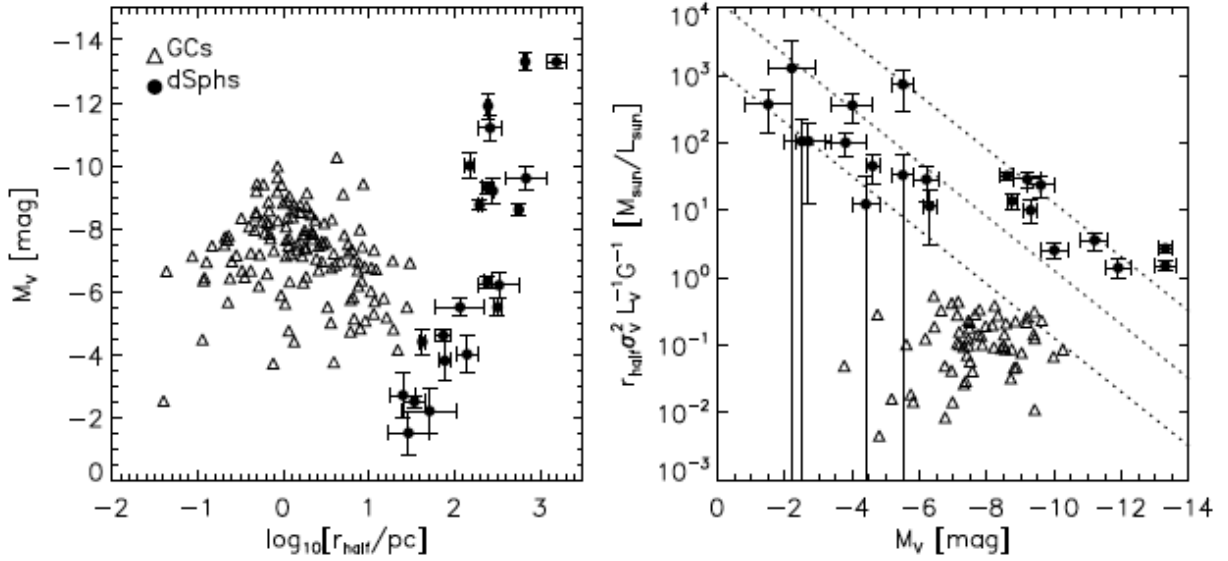


Fig. 13.— *Left*: Luminosity versus size (updated from Belokurov et al. 2007; Gilmore et al. 2007; Martin et al. 2008), for Milky Way satellites including objects classified as globular clusters (open triangles; data from Harris (1996, 2010 edition)) and dwarf spheroidals (filled circles with error bars; data from compilations by Irwin & Hatzidimitriou 1995; Mateo 1998; Martin et al. 2008; Sand et al. 2011). The apparent lack of objects toward low luminosity and large size is a selection effect that reflects the surface-brightness limit of the SDSS survey (Koposov et al. 2008). *Right*: Dynamical mass-to-light ratio (modulo a constant scale factor) versus luminosity. Updated from Mateo et al. (1993); Mateo (1998); Simon & Geha (2007); Geha et al. (2009). Dotted lines correspond to constant masses of $10^5 M_{\odot}$, $10^6 M_{\odot}$ and $10^7 M_{\odot}$.

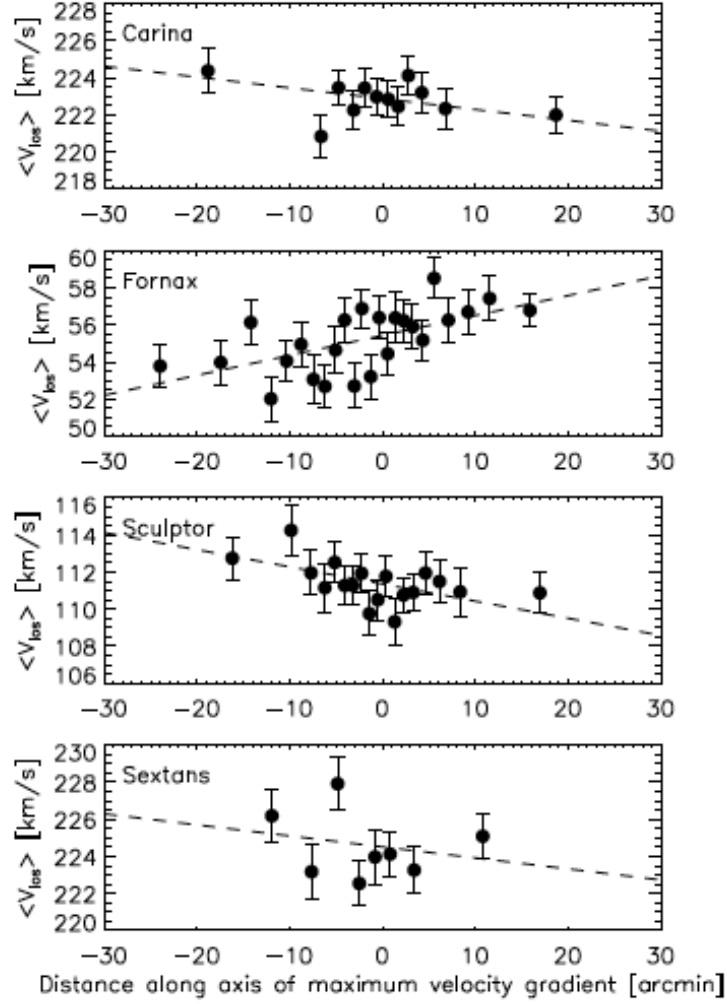


Fig. 14.— Line-of-sight velocity gradients in the Milky Way’s ‘classical’ dSph satellites. Panels display mean velocity as a function of distance along the axis corresponding to the maximum velocity gradient, from the samples of Walker, Mateo & Olszewski (2009). The observed gradients give rise to maximum amplitudes $R_{\max} dV/dR \lesssim 3 \text{ km s}^{-1}$, significantly less than the velocity dispersions ($\sigma \sim 10 \text{ km s}^{-1}$). Using VLT spectra from the DART survey, Battaglia et al. (2008) report similar results for Sculptor, measuring a gradient of $7.6^{+3.0}_{-2.2} \text{ km s}^{-1} \text{ deg}^{-1}$ along the morphological major axis.

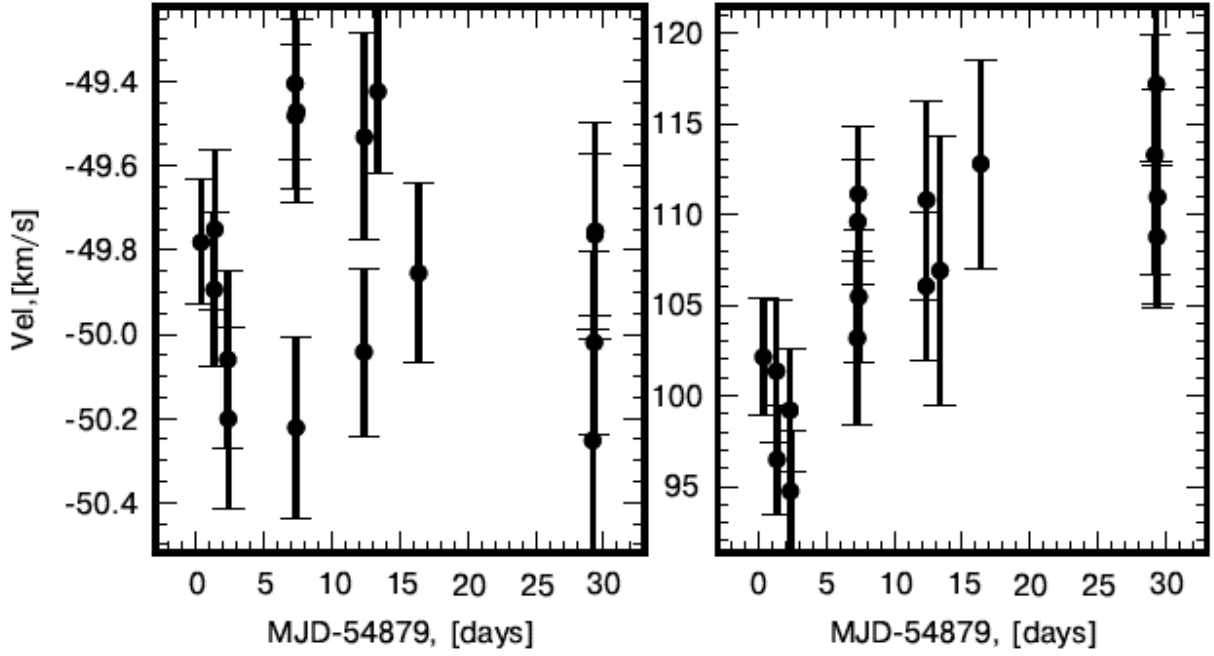


Fig. 15.— Direct detection of binary stars from individual velocity measurements in Boötes I (Koposov et al. 2011b, reproduced by permission of the American Astronomical Society). *Left*: foreground star with velocities consistent with a constant value. *Right*: member star ($\langle v \rangle_{\text{Boo}} \sim 105 \text{ km s}^{-1}$) exhibiting a velocity increase of $\sim 10 \text{ km s}^{-1}$ over one month. See section 3.3 for a discussion of the effects of binary orbital motions on measurements of dSph velocity dispersions.

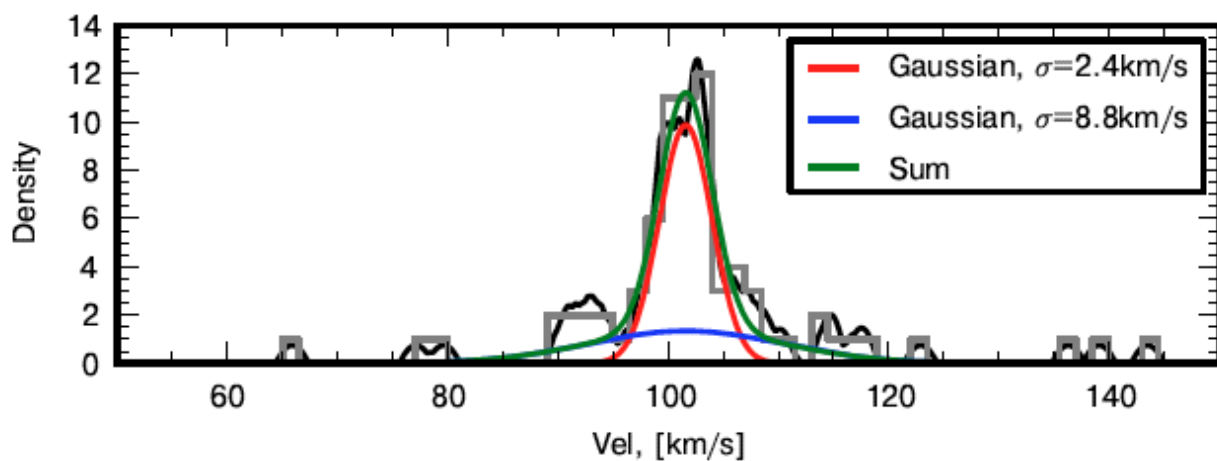


Fig. 16.— Velocity distribution of the Boötes I dSph, from the VLT/FLAMES data of Koposov et al. (2011b, reproduced by permission of the American Astronomical Society), not including 11 stars observed to have significant velocity variability. In the best-fitting two-Gaussian model, 70% of the stars belong to a ‘cold’ component with $\sigma \sim 2 \text{ km s}^{-1}$ and the rest belong to a hotter component with $\sigma \sim 9 \text{ km s}^{-1}$.

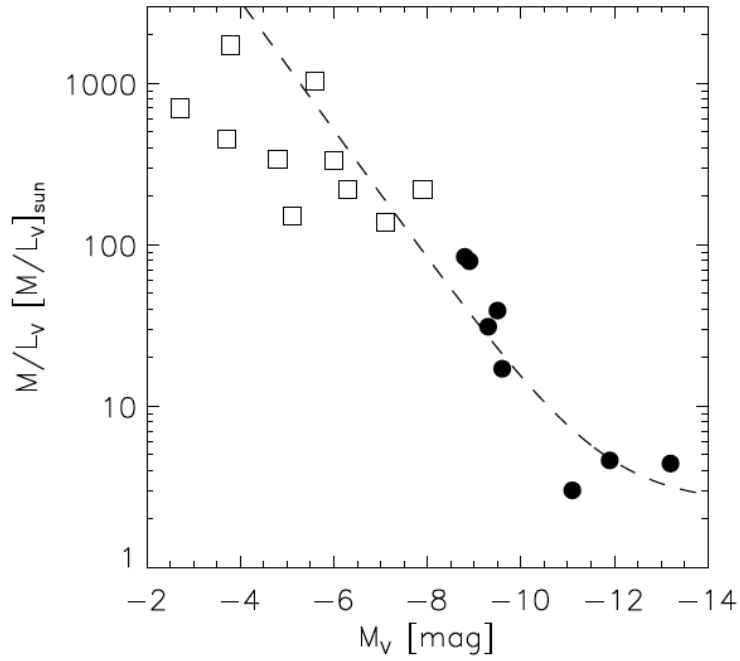


Fig. 17.— Dynamical mass-to-light ratio, derived from mass-follows-light models (Section 4.1.1), versus luminosity. Data for the Milky Way’s ‘classical’ dSphs (filled circles) are from the review of Mateo (1998). Data for the ‘ultrafaint’ dSphs (open squares) are from Keck/DEIMOS observations by Simon & Geha (2007) and Martin et al. (2007). The dotted line corresponds to $[M/L_V/[M/L_V]_{\odot}] = 2.5 + 10^7/(L/L_{V,\odot})$ (Section 5).

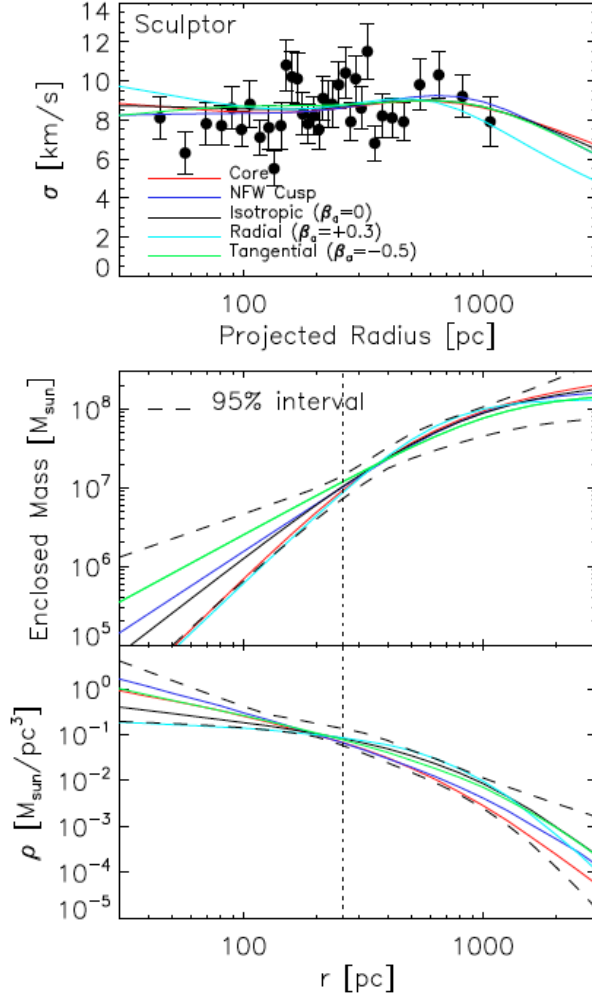


Fig. 18.— Degeneracy in the Jeans analysis of dSph mass profiles (Section 4.1.3). In the top panel, overplotted on Sculptor’s empirical velocity dispersion profile are best-fitting cored ($\gamma = 0$ in the notation of Equation 12) and cusped ($\gamma = 1$) density profiles, as well as models that assume isotropic ($\beta_a = 0$), radially anisotropic ($\beta_a = +0.3$) and tangentially anisotropic ($\beta_a = -0.5$) velocity distributions. All of these models provide equivalent fits to the data. The bottom two panels plot mass and density profiles corresponding to each model. Dotted curves indicate 95% confidence intervals, as determined from a Jeans/MCMC analysis that assumes constant anisotropy and lets the unspecified parameters in Equation 12 vary freely (Section 4.1.3). The vertical dotted line indicates Sculptor’s projected halflight radius.

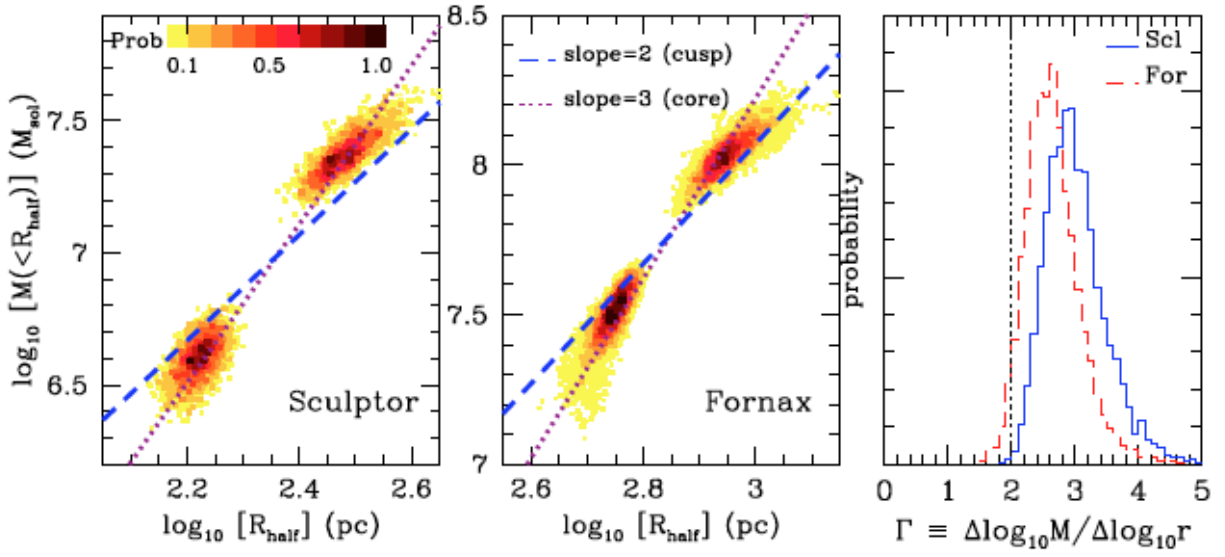


Fig. 19.— Empirical constraints on the slopes of mass profiles in Fornax and Sculptor, based on estimates of $M(r_h)$ for each of two chemo-dynamically independent stellar sub-populations in each galaxy (Section 4.2.3, Walker & Peñarrubia 2011, reproduced by permission of the American Astronomical Society). Points in the left two panels indicate constraints on the two half-light radii and masses enclosed therein, with lines indicating the maximum slopes allowed for cored ($\gamma = 0$ in the notation of Equation 12; $\Gamma \equiv \Delta \log M / \Delta \log r \leq 3$) and cusped ($\gamma = 1$, $\Gamma \leq 2$) overplotted. The right-hand panel indicates posterior probability distributions for the slope in each galaxy. The data rule out the cuspy ($\gamma \gtrsim 1$, $\Gamma \leq 2$) profiles that characterise the cold dark matter halos produced in cosmological simulations (e.g., Navarro, Frenk & White 1997) with significance $\gtrsim 96\%$ and $\gtrsim 99\%$ in Fornax and Sculptor, respectively.

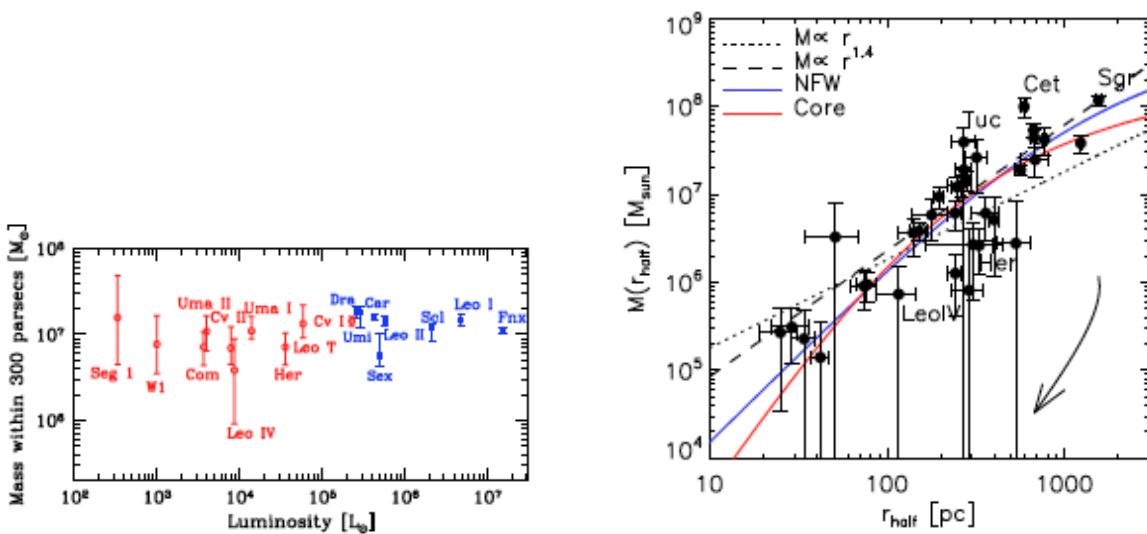


Fig. 20.— A common mass? *Left*: mass enclosed within a radius of $r \leq 300$ pc, estimated from a Jeans analysis (See Section 4.1.3), versus luminosity (Strigari et al. 2008a, reproduced with permission). *Right*: mass enclosed within the projected halfflight radius, estimated from Equation 15, versus halfflight radius (Walker et al. 2009b, reproduced by permission of the American Astronomical Society). Arrows indicate the trajectory followed by a satellites as they lose up to 99% of their original stellar mass, from N-body simulations by Peñarrubia et al. (2008). Overplotted are various dark matter halo models (Walker et al. 2009b).

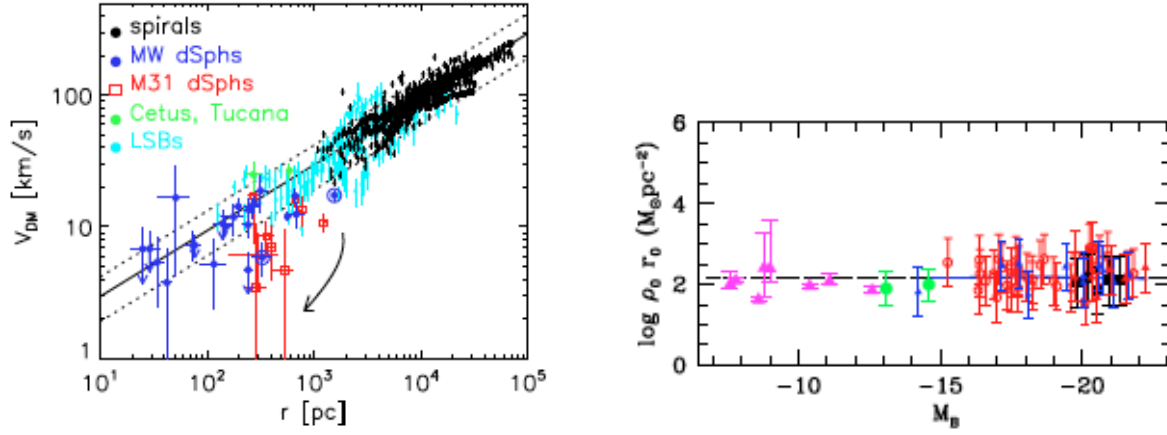


Fig. 21.— Similarity with spiral galaxies (Section 5)? *Left*: circular velocities ($v_{\text{circ}} = \sqrt{GM(R_h)/R_h}$) for the Milky Way’s dSph satellites lie on the extrapolation of the mean rotation curve due to dark matter in spiral (McGaugh et al. 2007) and low surface brightness (Kuzio de Naray et al. 2008) galaxies (Walker et al. 2010, reproduced by permission of the American Astronomical Society). *Right*: Dark matter surface densities inferred from fits of Burkert (1995) halos have the same constant value inferred from spiral galaxy rotation curves (reproduced from *Dwarf Spheroidal Galaxy Kinematics and Spiral Scaling Laws*, by P. Salucci et al., MNRAS, in press, by permission of John Wiley & Sons Ltd.).

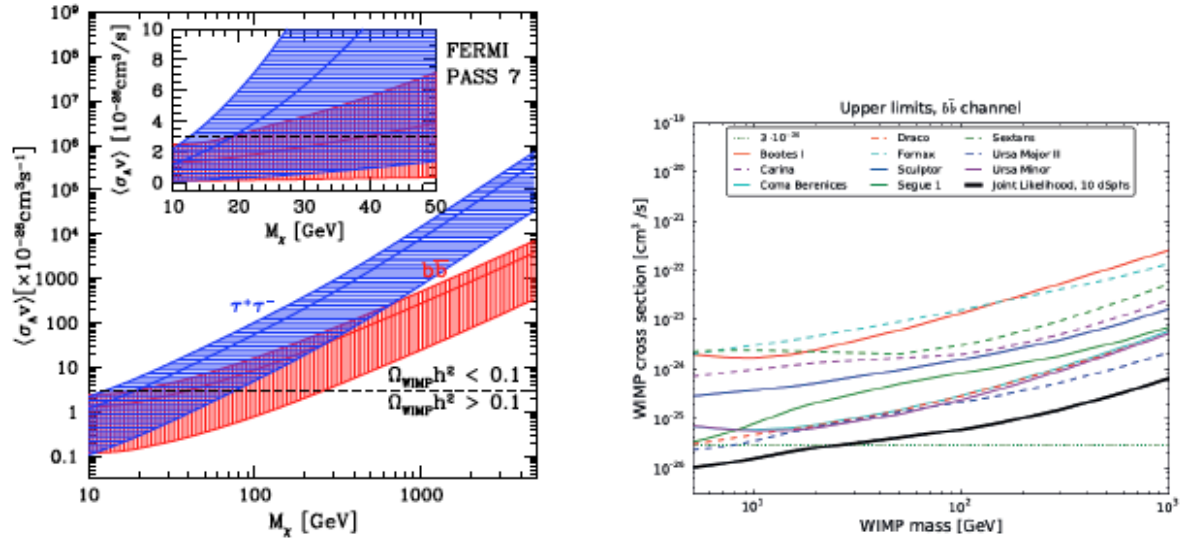


Fig. 22.— Exclusion of WIMP self-annihilation cross sections, based on Fermi-LAT non-detections (2-year data) of gamma-rays in the Milky Way’s dSph satellites (reprinted with permission from Geringer-Sameth & Koushiappas, Phys. Rev. Lett. 107, 241303 (2011; left) and Ackermann et al. (The Fermi Collaboration), Phys. Rev. Lett. 107, 241302 (2011; right), Copyright 2011 by the American Physical Society).